

# The Battle for Grid Flexibility

Control architectures, information gaps, and grid optimization

Mads R. Almassalkhi, Ph.D.

*Chief Scientist  
(joint appointment)*



*Associate Professor  
Electrical Engineering*



*Co-founder*



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**Electric Energy  
Systems Group**

# Acknowledgements

## *Active/recent collaborators*

- Prof. Pierre Pinson (Imperial)
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- Dr. Soumya Kundu (PNNL/UVM)
- Dr. Sam Chevalier (DTU/UVM)
- Prof. Amrit Pandey (UVM)
- Prof. Hamid Ossareh (UVM)
- Prof. Luis Duffaut Espinosa (UVM)
- Dr. Paul Hines (EnergyHub)
- Prof. Jeff Frolik (UVM)
- Dr. Sarnaduti Brahma (Siemens)
- Prof. Sumit Paudyal (FIU)
- Prof. Dennice Gayme (JHU)
- Prof. Enrique Mallada (JHU)
- Dr. Dhananjay Anand (JHU)
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- Dr. Alexander Engelmann (TU-Dortmund)
- Prof. Roland Malhamé (Poly Montreal)
- Dr. Ning Qi (Tsinghua)
- Prof. Ian Hiskens (UMICH)
- Prof. Johanna Mathieu (UMICH)

## *Current group members*

- Dr. Tanmay Mishra (Post-doc)
- Mr. Hani Mavalizadeh (PhD student)
- Mr. Waheed Owonikoko (PhD Student)
- Mr. Mazen El-Saadany (PhD Student)
- Ms. Rebecca Holt (undergraduate researcher)
- Ms. Emily Ninestein (undergraduate researcher)
- Ms. Kendall Meinhofer (undergraduate researcher)

## *Group Alumni*

- Dr. Adil Khurram (PhD EE'21) → Scientist @ UCSD (San Diego, CA)
- Dr. Nawaf Nazir (PhD EE'20) → Research @ PNNL (Richland, WA)
- Dr. Mahraz Amini (PhD EE'19) → Strategy @ NatGrid (Dallas, TX)
- Mr. Micah Botkin Levy (MSEE'19) → Modeling @ Form Energy (SF, CA)
- Mr. Zach Hurwitz (MSME'19) → Energy @ Siemens (ME)
- Mr. Lincoln Sprague (MSEE'17) → Compliance @ Dynapower (VT)
- Ms. Anna Towle (BSEE'16) → Trader @ Fortum (Sweden)



# VECTORS: interdisciplinary Energy & Autonomy group

**Objective:** sustain and strengthen UVM's research impact in the area of understanding, controlling, and optimizing sustainable, resilient, and autonomous systems and networks by leveraging a group of diverse, interdisciplinary, and research-active faculty.



Mads R. Almassalkhi  
(Founding Director)



Jeff Frolík



Amrit Pandey



Bindu Panikkar



Hamid Ossareh



James Bagrow



Luis D. Espinosa



Jeff Marshall



Sam Chevalier  
(Starts Aug 2023)

## Broad expertise

- Energy justice
- Power/energy systems
- Grid modeling
- Optimization
- Control theory
- Network science
- IoT/Comms
- Data science
- Machine learning



# Impactful R&D with industry & research partners

Recent and ongoing industry-supported projects with



Sandia  
National  
Laboratories



GLOBAL  
FOUNDRIES



Pacific Northwest  
NATIONAL LABORATORY

Recent and ongoing funding partners





# Recent success with translational research

## Packetized Plug-in Electric Vehicle Charge Management

Pooya Rezaei, *Student Member, IEEE*, Jeff Frolik, *Senior Member, IEEE* and Paul Hines, *Member, IEEE*

known as smart charging) methods is one step to facilitate the

## Packetized energy management: asynchronous and anonymous coordination of thermostatically controlled loads

Mads Almssalkhi, *Member, IEEE*

Jeff Frolik, *Senior Member, IEEE*

Paul Hines, *Senior Member, IEEE*



**Abstract**—Because of their internal energy storage, electrically powered, distributed thermostatically controlled loads (TCLs) have the potential to be dynamically managed to match their aggregate load to the available supply. However, in order to facilitate consumer acceptance of this type of load management, TCLs need to be managed in a way that avoids degrading perceived quality of service (QoS), autonomy, and privacy. This paper presents a real-time, adaptable approach to managing TCLs that both meets the requirements of the grid and does not require explicit knowledge of a specific TCL's state. The method leverages a packetized, probabilistic approach to energy delivery that draws inspiration from digital communications. We demonstrate the packetized approach using a case-study of 1000 simulated water heaters and show that the method can closely track a time-varying reference signal without noticeably degrading the QoS. In addition, we illustrate how placing a simple ramp-rate limit on the aggregate response overcomes synchronization effects that arise under prolonged peak curtailment scenarios.

"fairness" properties with regard to providing statistically identical grid access to each load.

With the proposed PEM architecture, the grid operator or aggregator only requires a two dimensional measurement from the collection of loads: aggregate power consumption and an aggregate request process. This represents a significant advantage over aggregate model-estimator-controller state-space approaches in [4], which requires an entire histogram of states from the collection of loads to update a state bin transition model. In [4], this is addressed through an observer design to estimate the histogram based on aggregate power consumption; however, in some cases, the model may not be observable [5]. Recent work has extended [4] to include higher order dynamic models and end-user and compressor delay constraints [6] and stochastic dynamical performance bounds [7]. Similar to the mean-field

+



=



Numerous academic papers+  
research projects+ IP +  
industry partners  
(2012-present)

Co-founded startup company  
(2016)

Company acquired! Technology  
now has access to scale:  
1,000,000 devices  
(2022)



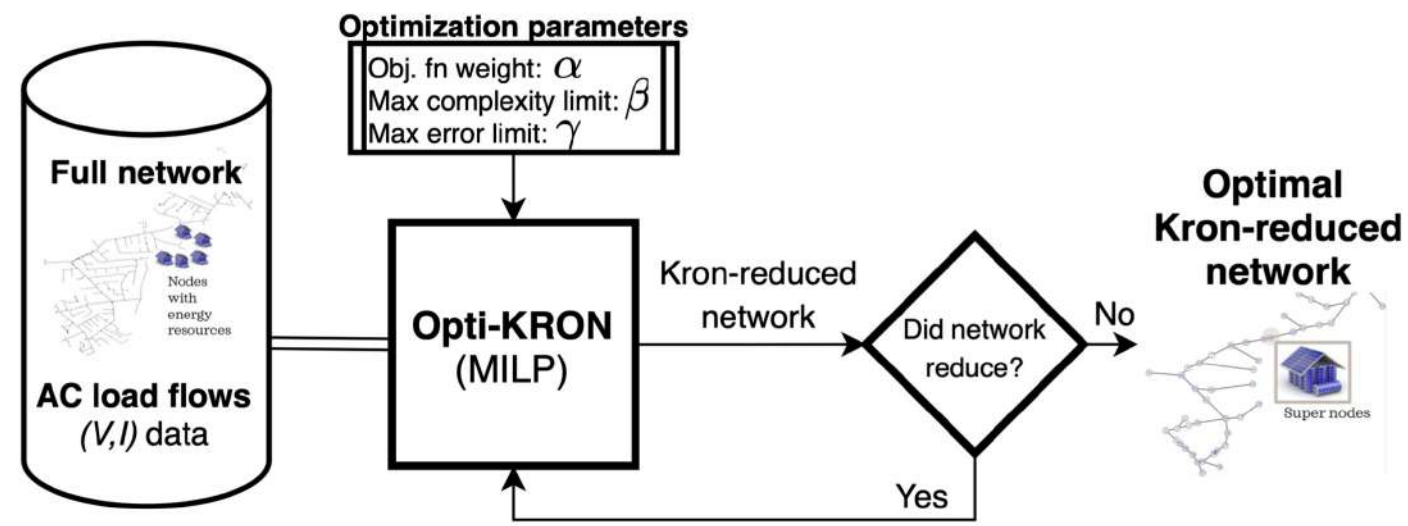
# Vermont is amazing platform for power/energy R&D

- ✓ Population: 650,000 people with a peak load of ca. 1GW
  - ▶ AMI deployed at >95% of customers in State
  - Vermont Renewable Portfolio Standard (RPS): 75% by 2032*
- ✓ Small state → easy to collaborate, test ideas, create change, make an impact
- ✓ Close partnerships with nationally-recognized innovative industries
  - ▶ *VELCO, GMP, BED, VEIC, Dynapower, Vermont Gas, Beta Technologies, etc.*
- ✓ Joint appointment program with national lab (PNNL)
- ✓ Strong presence with competitive federal E programs
  - ▶ *Past funding from ARPA-E NODES, SETO ENERGISE, NSF CAREER, CRISP, DOE GMLC*
- ✓ Outstanding interdisciplinary collaborations with the UVM Complex Systems Center and Gund Institute for Environment
- ✓ **VT is #2 state in U.S. for Clean Energy Momentum (UofCS, 2017)**
  - 5.4% of workforce is clean energy economy (#1 in 2021)
    - ▶ *Next largest are at ~3%*
  - 99.9% of VT *generation* is renewable (#1 in US in 2019)
  - 66% of consumed electricity is renewable (2019)
  - 15% of electricity from solar PV (#4 in US in 2020; #6 per capita)
  - 5.4% of new cars sold are EVs in 2021 (VT was #9 in 2018)

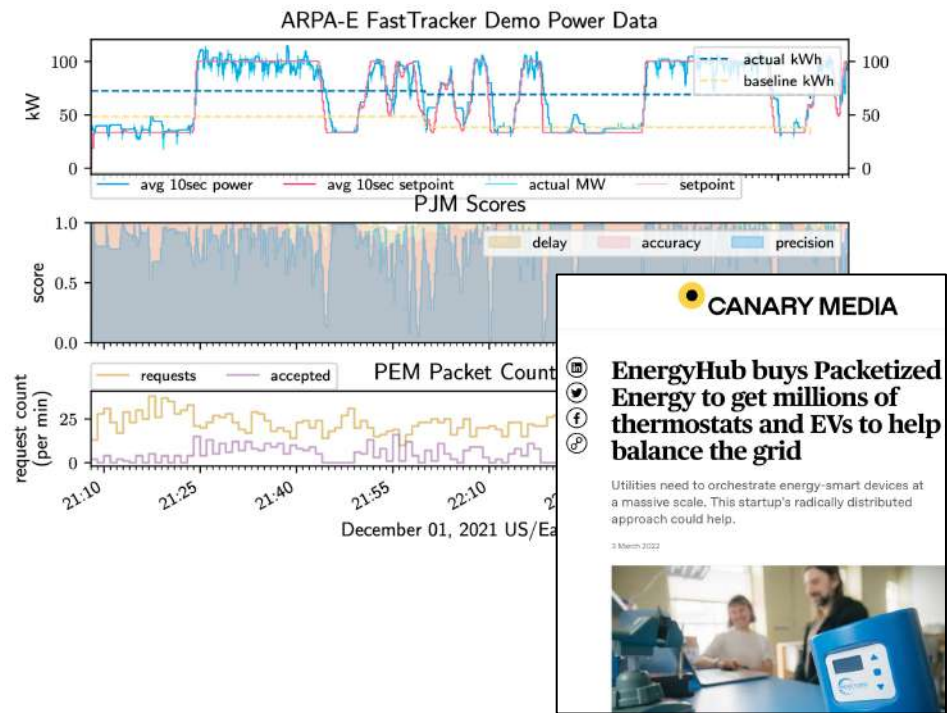


# What I will not talk about today

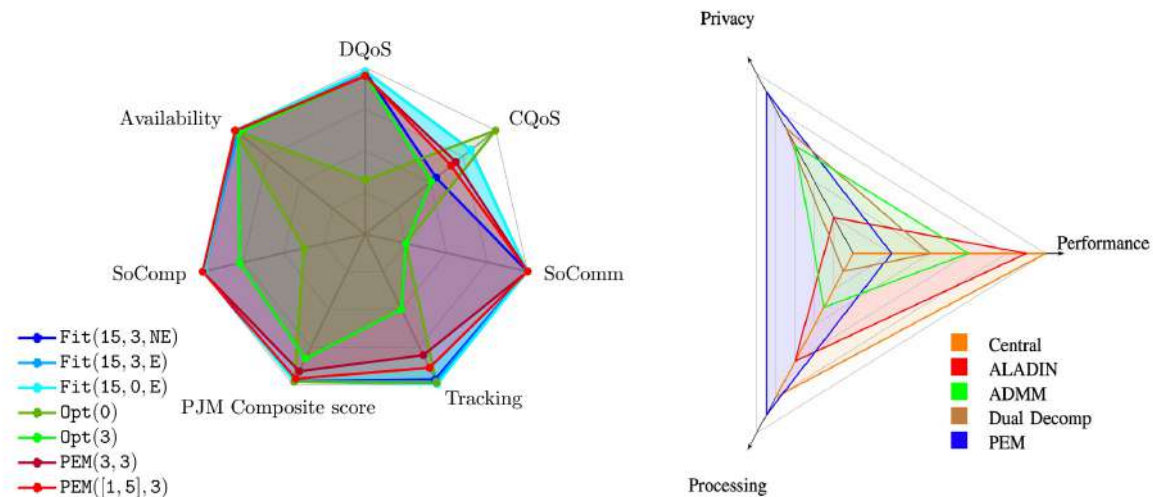
## Optimal (physics-informed) network reductions



## Packetized energy management



## Methodologies for characterizing DER algorithms



## Collision-free trajectory optimization of swarms





# Green economies are rising....



\$1.3T

Annual sales revenue

10M

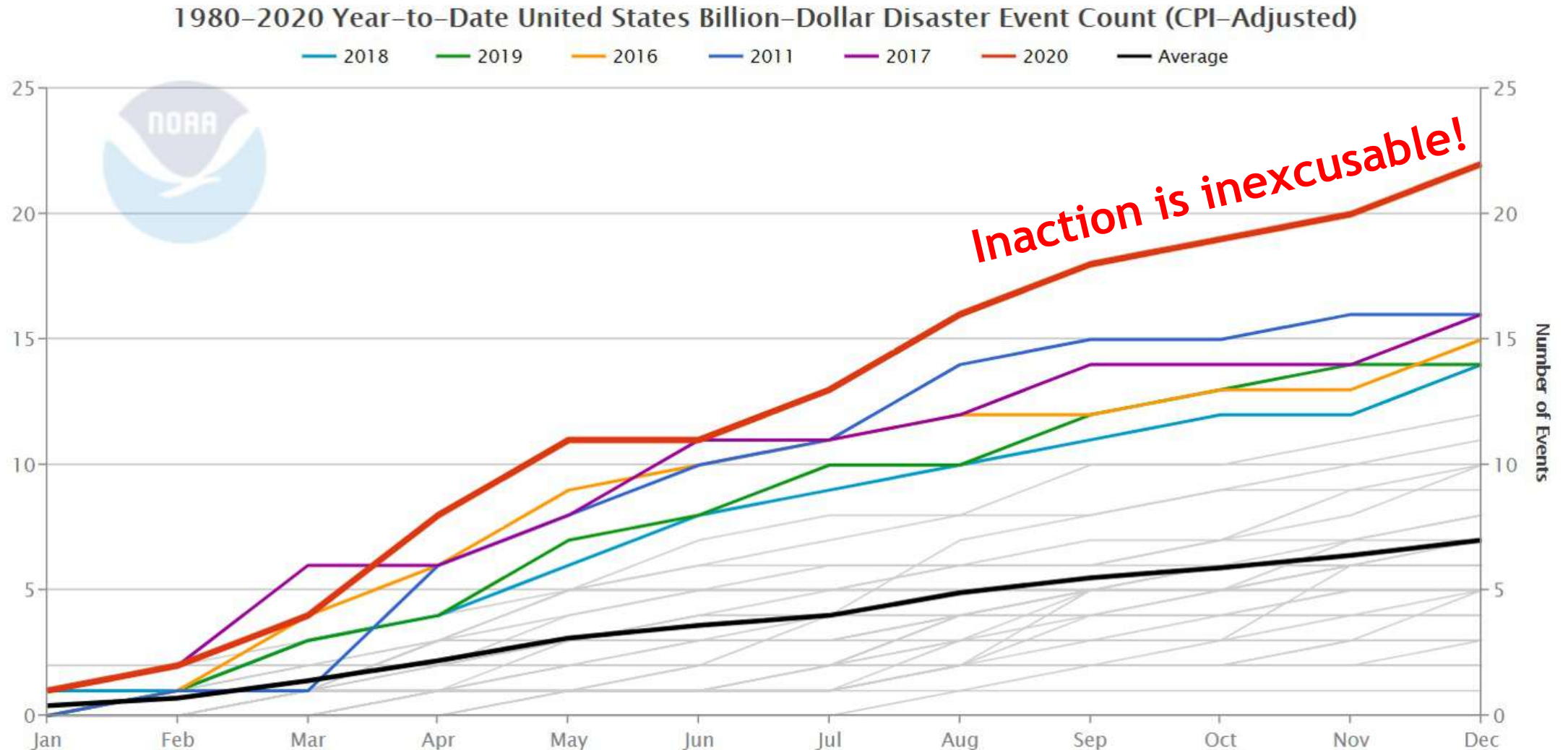
Jobs supported

*Green economy := environmental, low carbon and renewable energy activities*

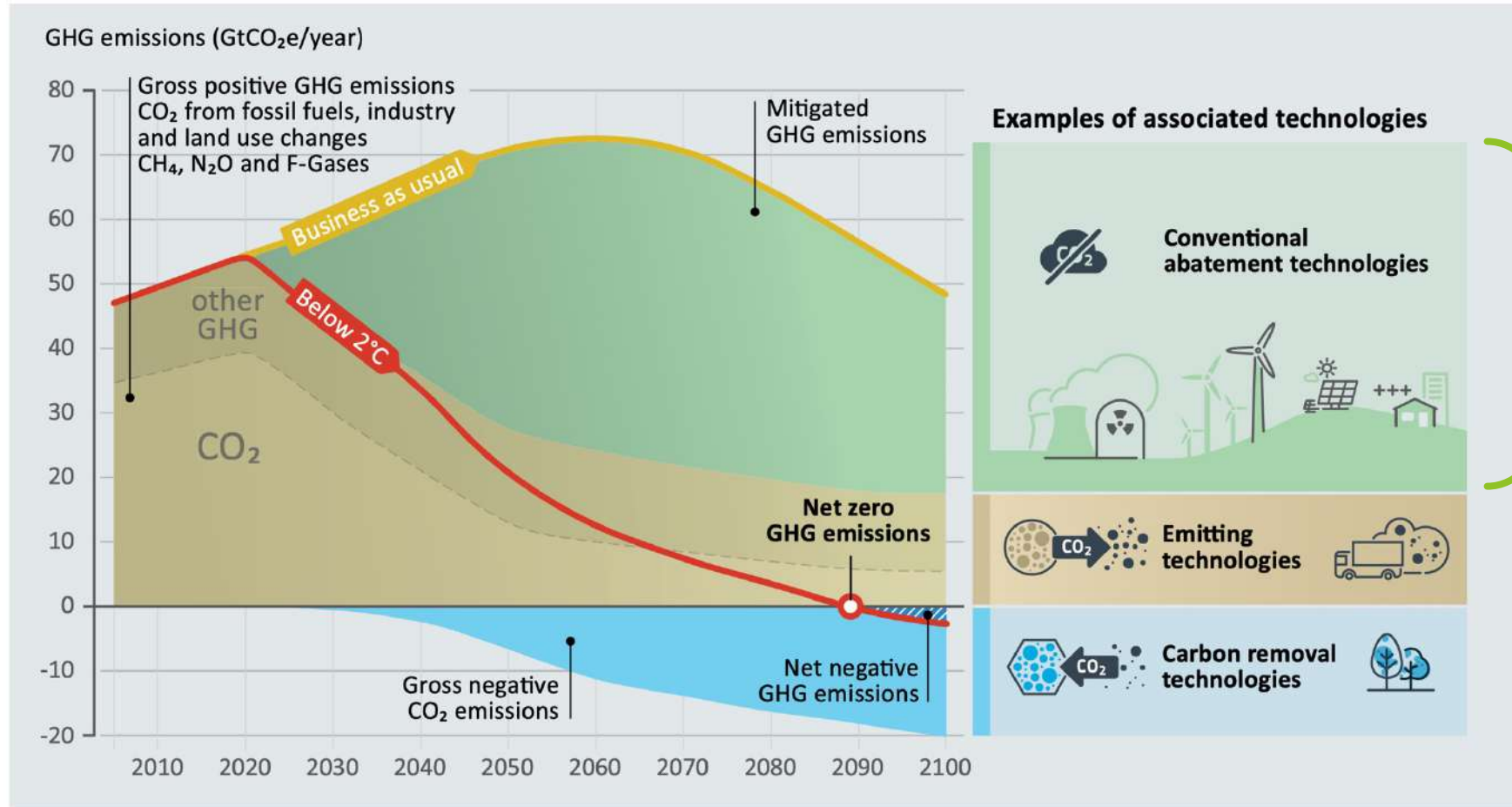




...but so are climate challenges



# Solutions? If they work, they will matter!



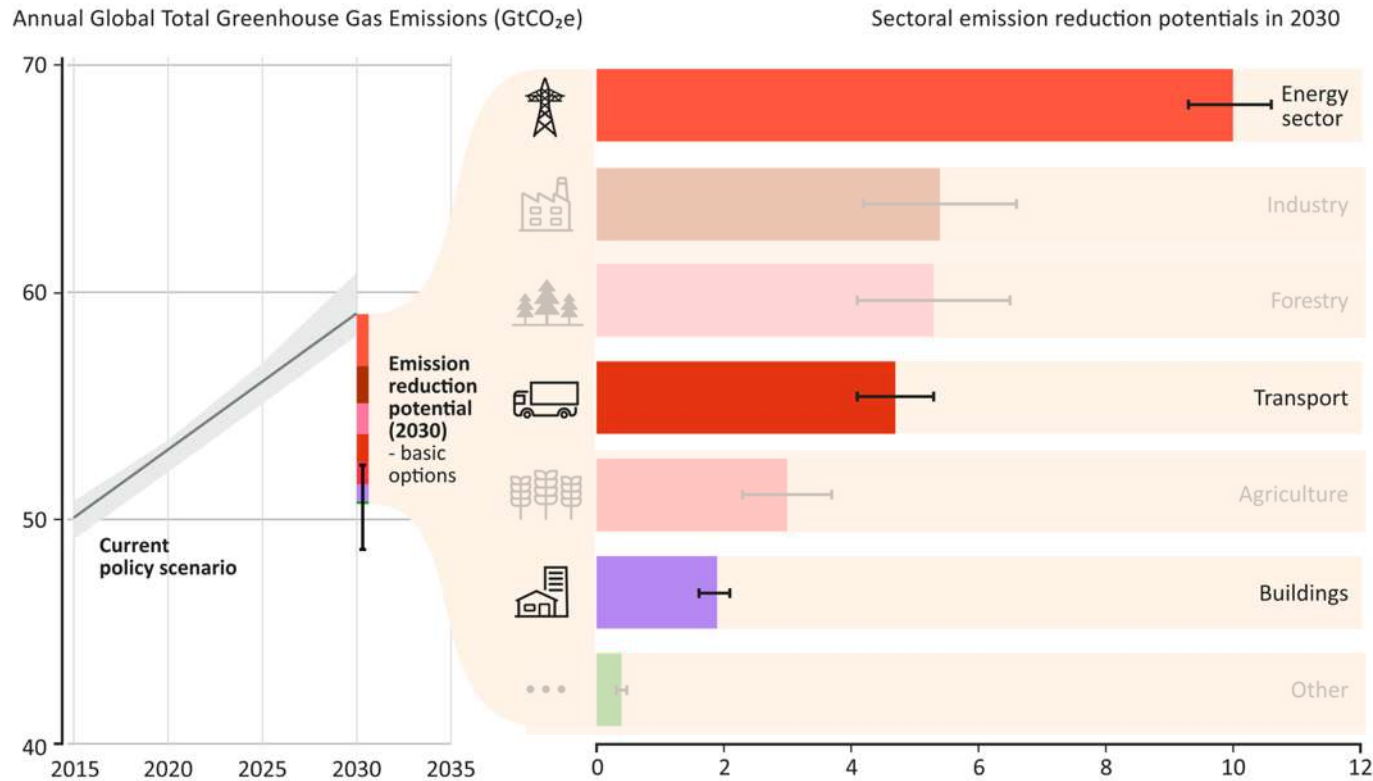
Requires massive  
TW-scale  
renewable  
integration

A massive  
power systems  
challenge!

**Key:** power systems is climate change mitigation engineering with a global impact!

# Flexibility can help: intelligent electrification

Energy, transportation, and building sectors are key!



Combine renewable and efficiency with **electrification of end use.** [1]

**Flexible demand enables significantly more renewable generation and reduces duck-curve ramping effects** [2]

**59GW of DR today will become 200GW of flexible demand by 2030** [3]

**Need to coordinate billions of energy resources!**

[1] UN Environmental Program, Emission Gap Report 2019 (source for figure, too)

[2] Goldenberg, et al, "Demand Flexibility: The Key To Enabling A Low-cost, Low-carbon Grid," Tech. Rep., Rocky Mountain Institute, 2018.

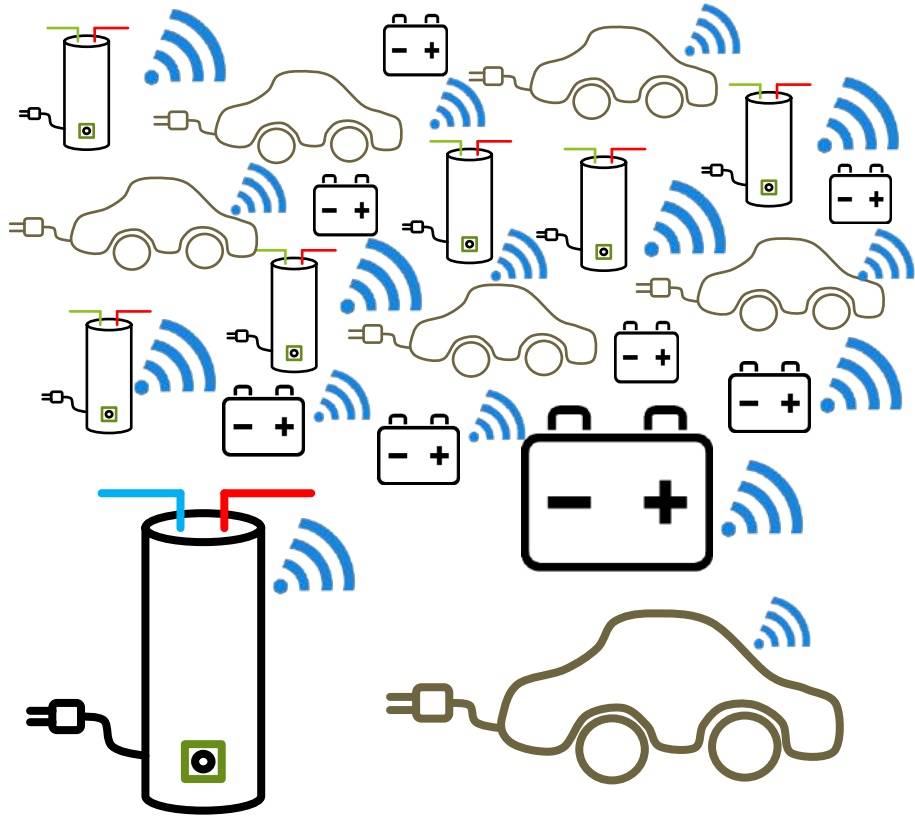
[3] Hledik et al, "The National Potential for Load Flexibility: Value And Market Potential Through 2030," Tech. Rep., The Brattle Group, 2019.





# Simple idea: turn connected loads into flexible demand

Demand-side DERs + communication + control



Every device, home, neighborhood, town, and state can become a dispatchable resource



# Value-stacking can be significant for flexibility

GRID BALANCING,  
ANCILLARY SERVICES



LMP ENERGY ARBITRAGE,  
RENEWABLE SMOOTHING



AVOIDED T&D CAPEX,  
NON-WIRES ALTERNATIVES,  
DIST. GRID MANAGEMENT



AVOIDED GEN CAPACITY



\$100 to \$1000  
per kW<sub>flex</sub> per year\*

Virtual power plant™  
*Virtual battery*™  
*Prosumer*™



TESLA

SUNRUN

GENERAC

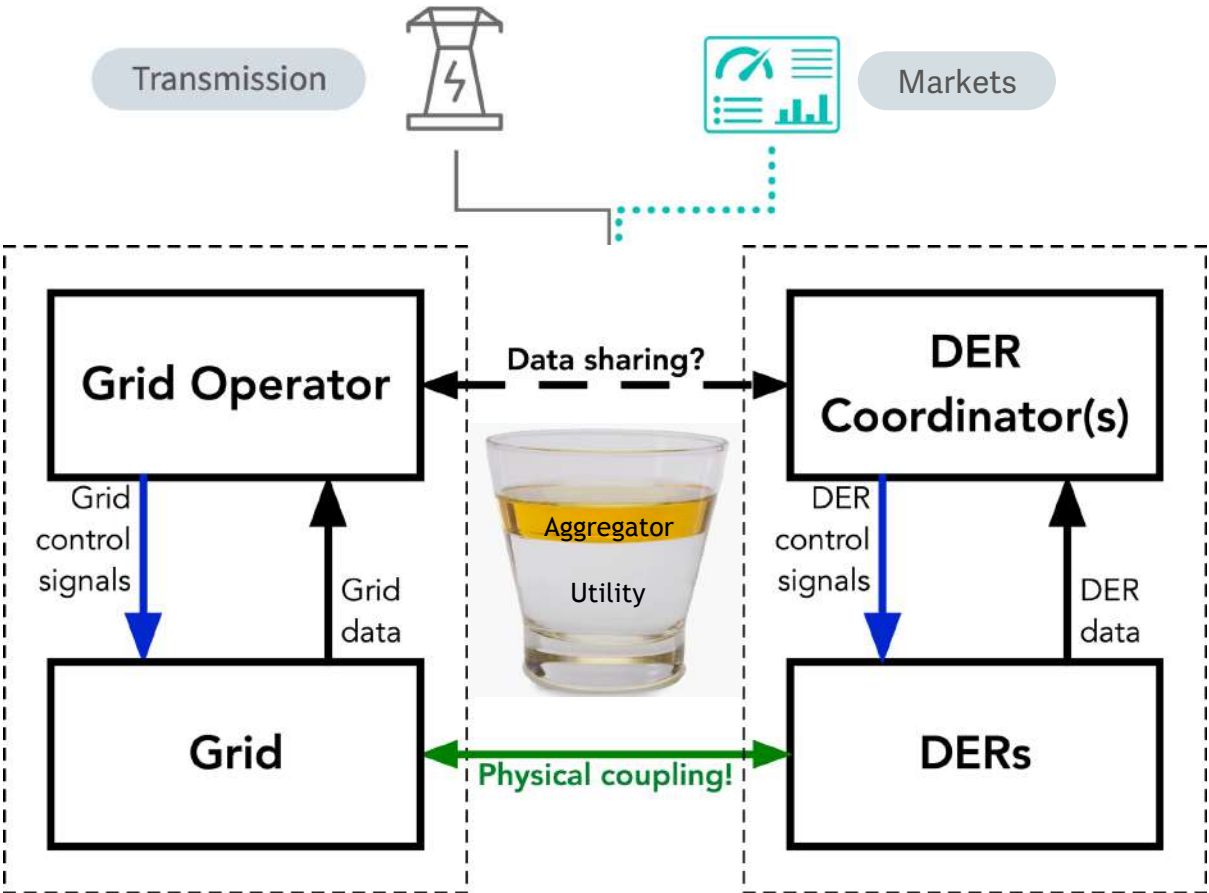
EnergyHub



\*Values from representative 2019 ISO New England market prices and services and from RMI/Brattle.

# DER coordination is ~~hard and complicated~~ fun

*Who knows what? Who controls what?*





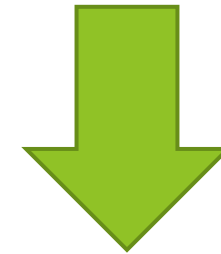
# How can we define *flexibility* ( $kW_{flex}$ )?

- ▶ Asset being responsive to (incentive/control) signals
  - ▶ Ability to defer/change (net) consumption?
  - ▶ *Flexibility* of a stand-alone battery is straight-forward



## Key parameters of a battery's flexibility

- State of charge (SoC)
- Ramp-rate (change in power)
- Net injections (power limits)
- Capacity (energy limits)



*How much power, how fast, and for how long?*  
➔ *Magnitude, response rate, and duration*

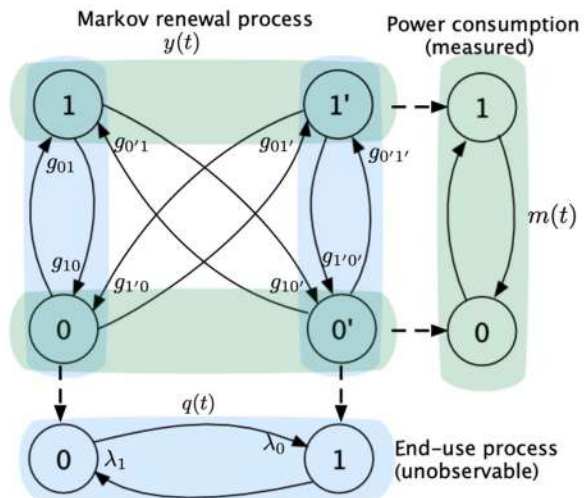


# For heterogenous mix of DERs, it's complicated!

1

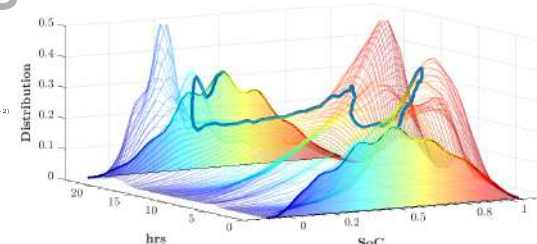
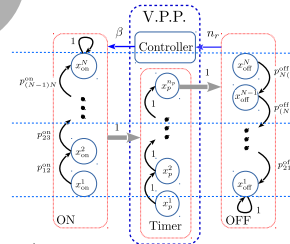
Stochastic end-use

Estimate background end-use needs (QoS)



2

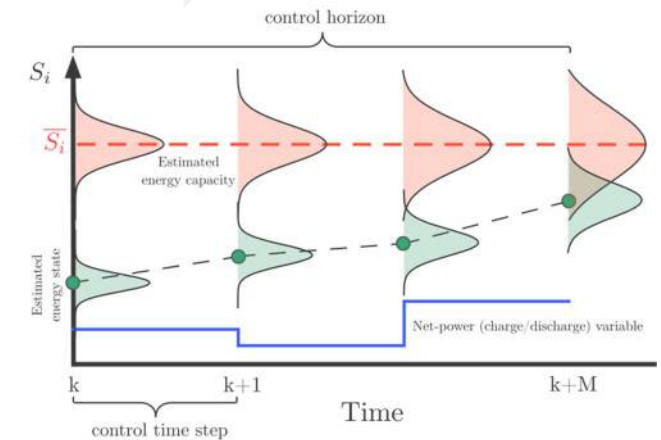
Modeling and control



3

Optimal dispatch

Uncertain resource



(1) A. Khurram, Luis Duffaut Espinosa, Roland Malhamé, Mads Almassalkhi, "Identification of Hot Water End-use Process of EWHs from Energy Measurements," EPSR, 2020

(2a) L. Duffaut and M. Almassalkhi, "A packetized energy management macromodel with QoS guarantees for demand-side resources," IEEE Trans. on Power Systems, 2021

(2b) L. Duffaut, A. Khurram, and M. Almassalkhi "Reference-Tracking Control Policies for Packetized Coordination of Heterogeneous DER Populations," IEEE Trans. on Control Systems Tech., 2021

(2c) L. Duffaut Espinosa, A. Khurram, and M. Almassalkhi, "A Virtual Battery Model for Packetized Energy Management," in IEEE Conference on Decision and Control (CDC), 2020

(3a) M. Amini and M. Almassalkhi, "Corrective optimal dispatch of uncertain virtual energy resources," IEEE Transactions on Smart Grid, 2020

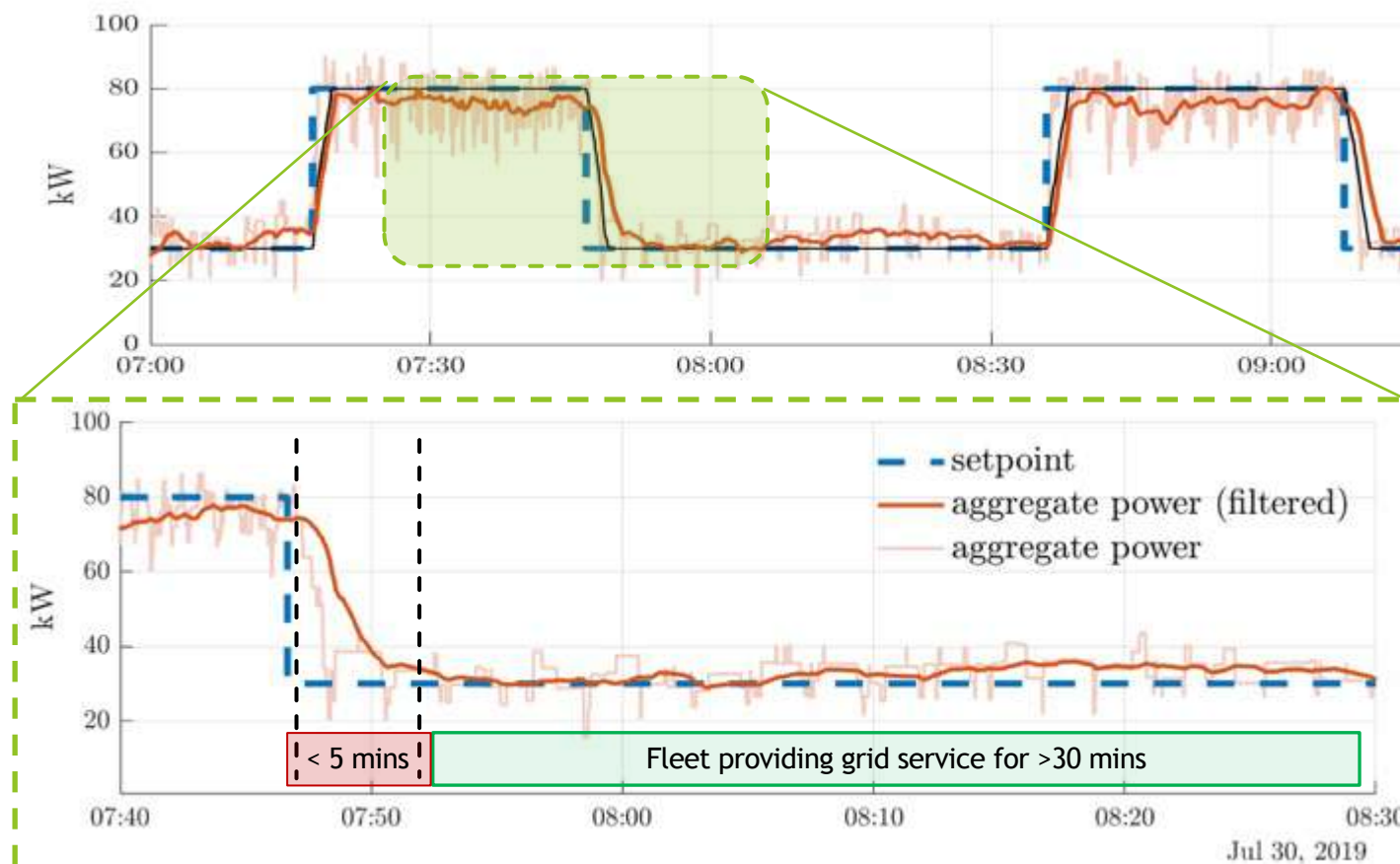
(3b) N. Qi, P. Pinson, M. Almassalkhi, et al, "Chance-constrained economic dispatch of generic energy storage under decision-dependent uncertainty," IEEE Trans. on Sust. Energy, 2023



# Example: field trial with coordinating 150 loads (2019)



The  
UNIVERSITY  
of VERMONT

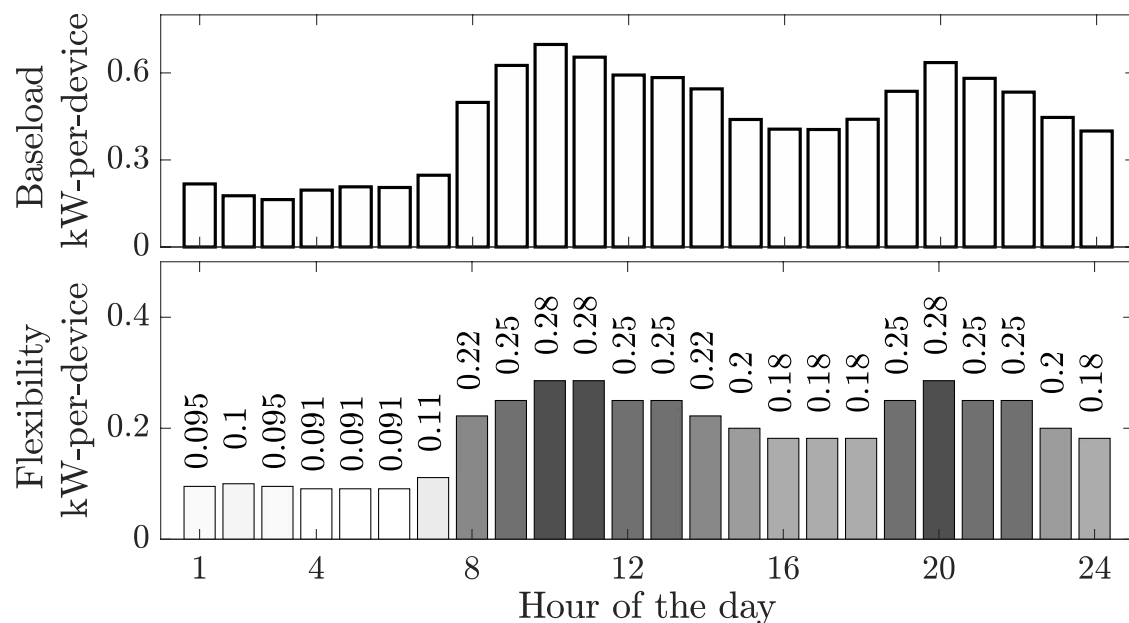


Dynamics depend on control architecture + parameters + end-users



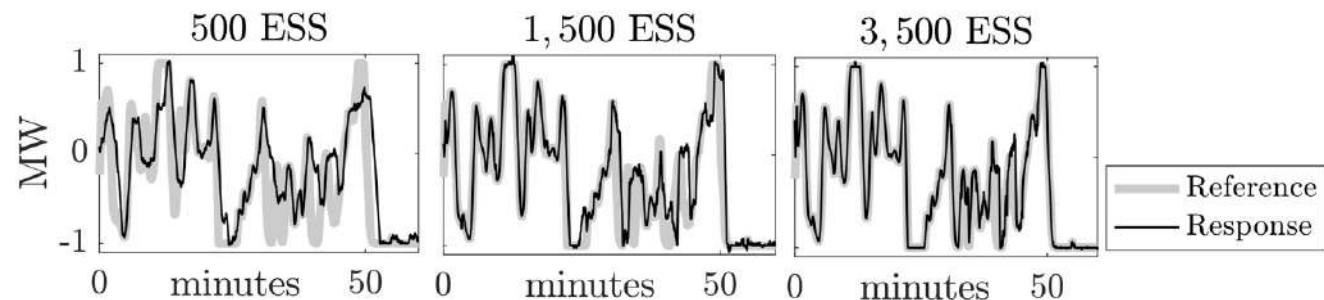
# How many DERs are needed for $\pm 1\text{MW}$ of freq reg?

## Electric water heaters

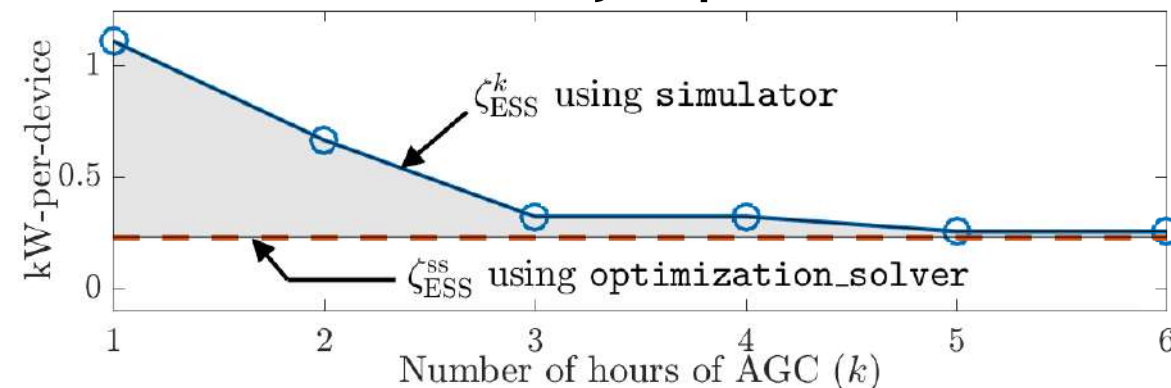


Up to 10,000 EWHs at night and 4000-5000 during day

## Batteries



## Available flexibility depends on duration

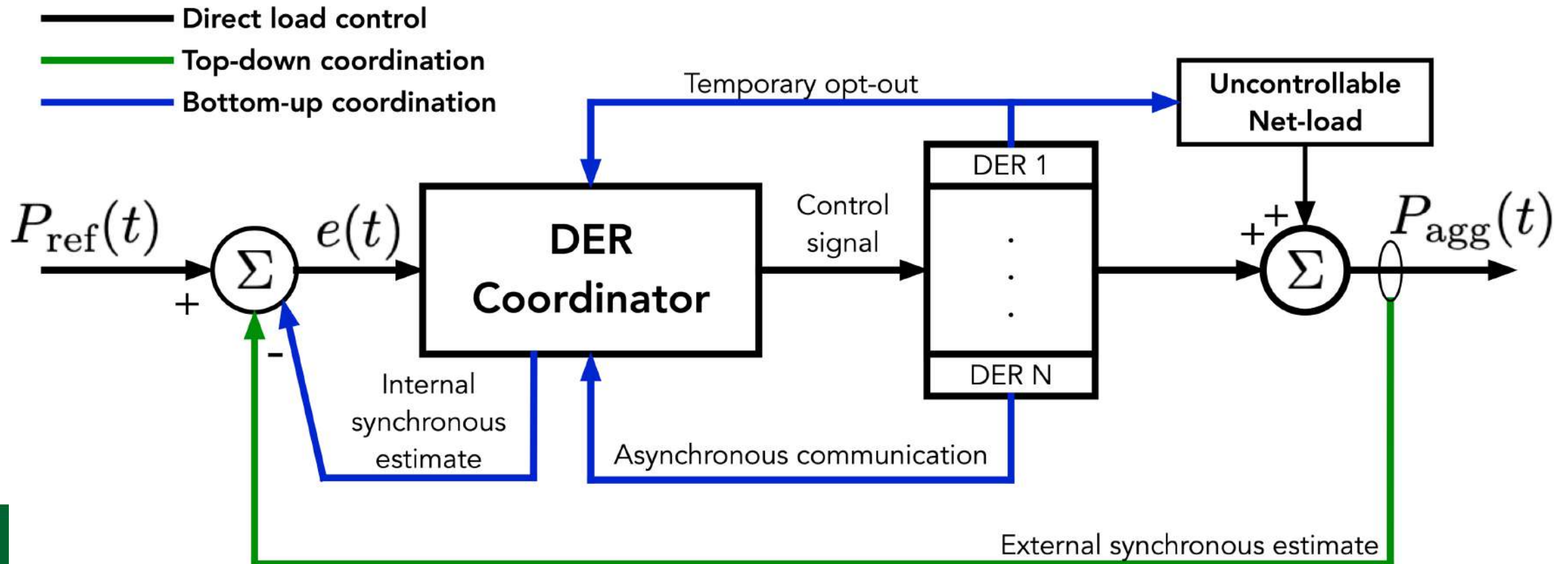


End-user behaviors & constraints and DER controller affect available flexibility

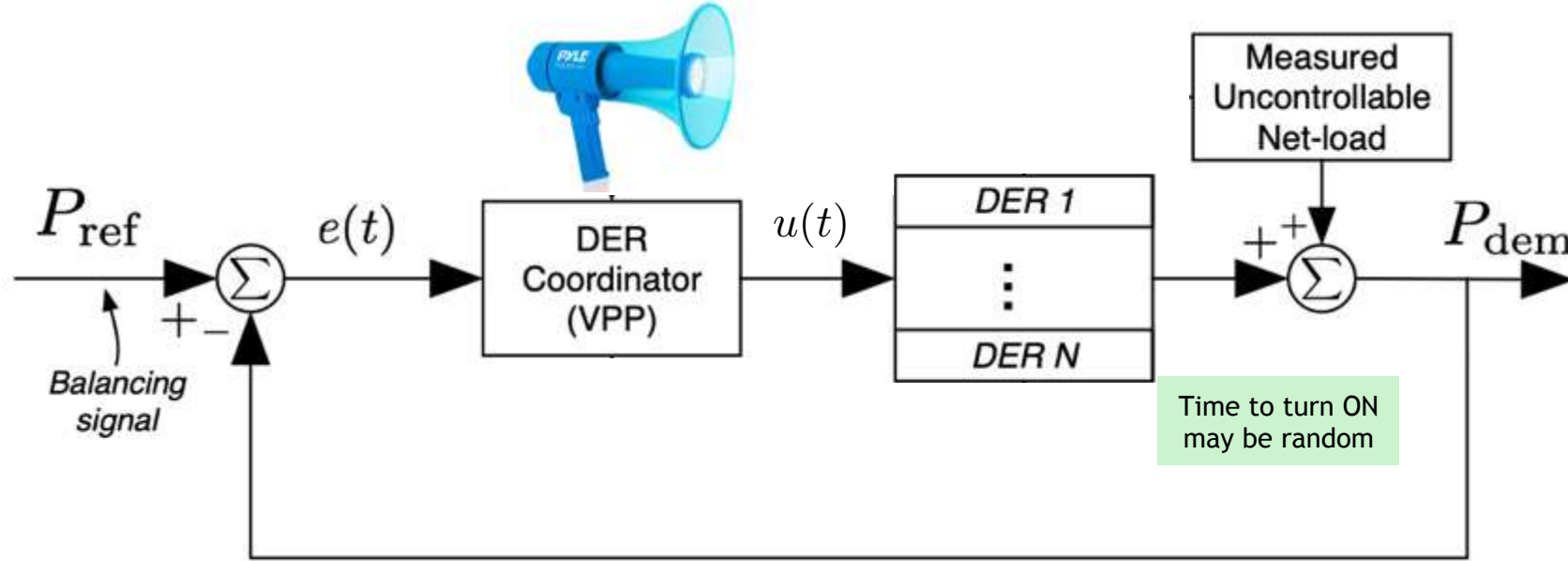


# DER coordination requires a control architecture

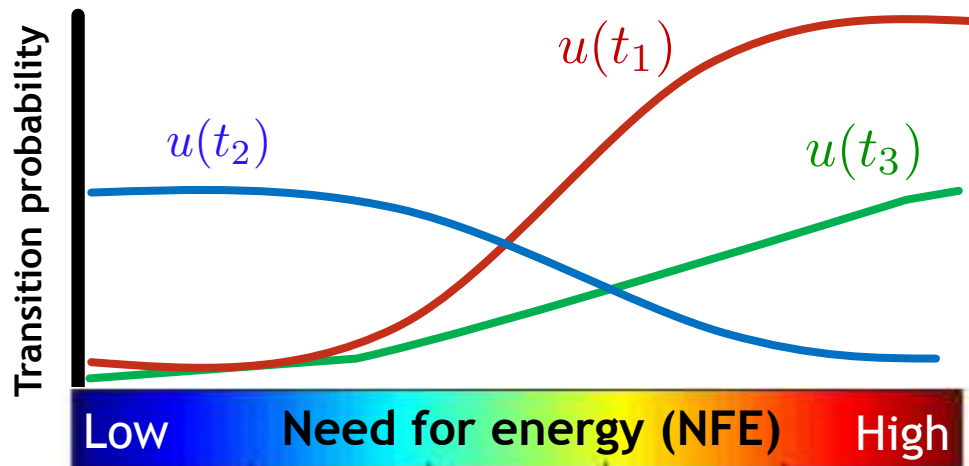
*How to control DERs? What's measured/estimated?*



# Architecture #1: Broadcast-based approach (top-down)



Local device logic can guarantee QoS



Broadcast control signal to all devices **synchronously**. Control signal is **explicit incentive (transactive)** or pdf.

**Requires feedback** from actual/estimated demand and/or having devices stream back data/status. Else is **open-loop**

**But** challenging to get feedback, hard to distinguish individual device constraints or grid locations (i.e., DER cycling and local grid conditions).



## Direct load control or TOU pricing (open-loop)

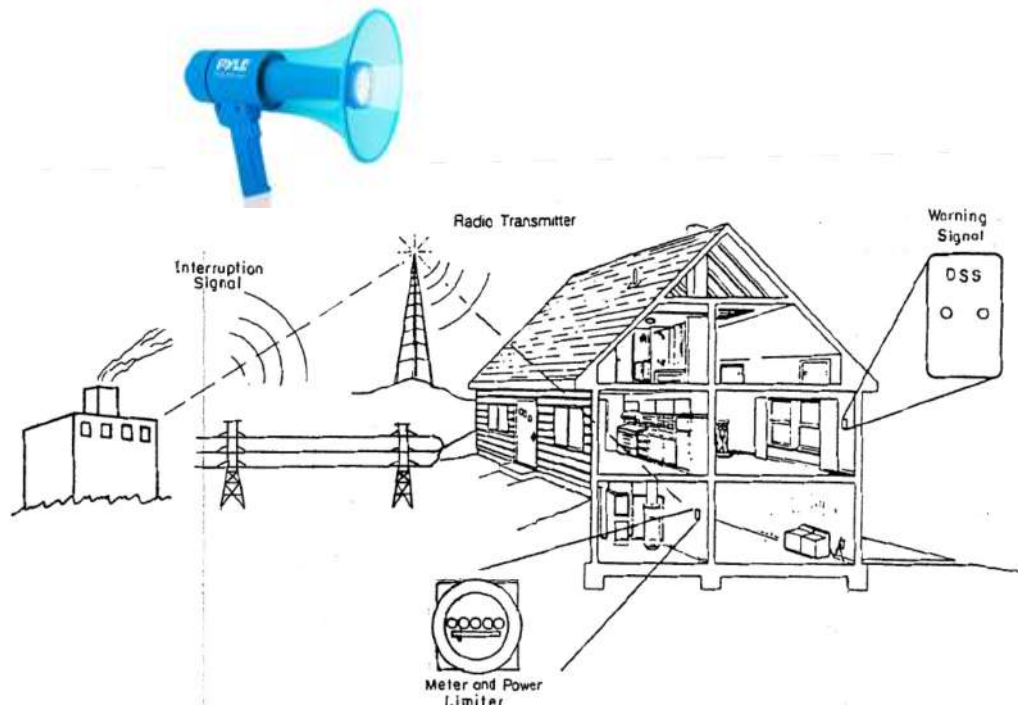
We can do better than  
sprinkler control



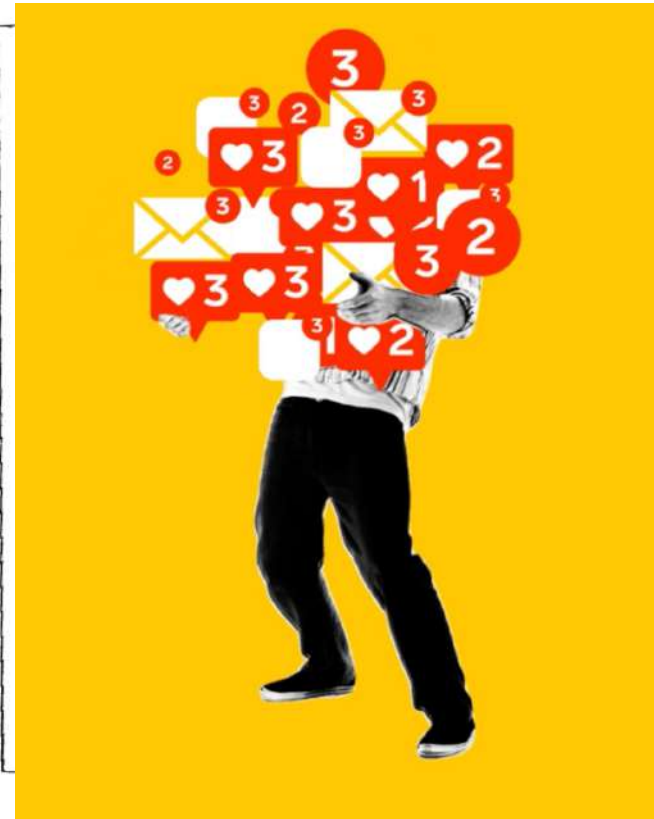


# Broadcast control example: California in 1982

**Demand subscription service (DSS):** radio-controlled fuse limits demand to subscribed level



Source: Shmuel Oren, 1982



*Today many utilities use SMS*

**Human becomes the actuator in-the-loop**

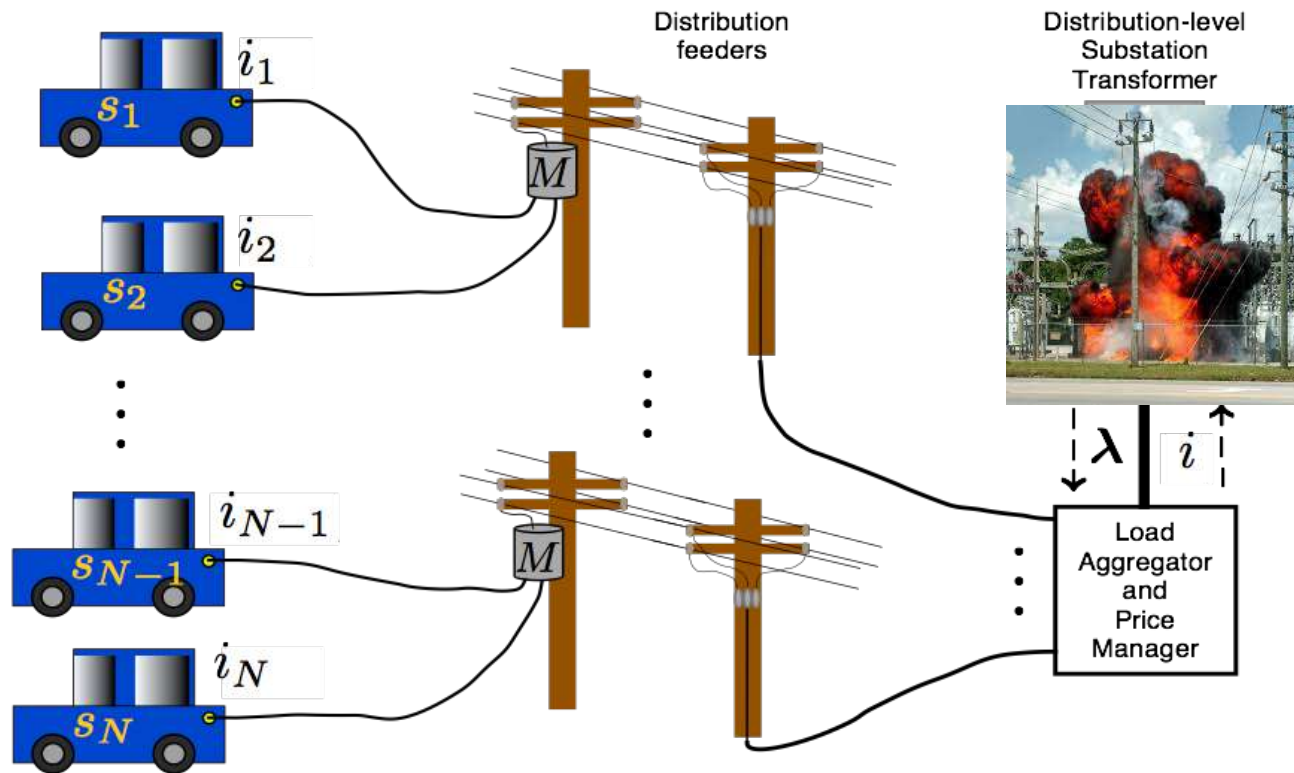


Source: VectorStock.com/7537816



# Illustrating indirect control: EV charging scenario

Consider a fleet of EVs served by a transformer (with dynamic temperature rating)



**EVs' objectives:** charge quickly!

$$s_n[k+1] = s_n[k] + \eta_n i_n[k]$$

**Transformer challenge:** uncoordinated charging  $\rightarrow$  **overload**  $\rightarrow$  insulation loss

**Transformer temperature:**  $T[k] \leq T^{\max}$

$$T[k+1] = \tau T[k] + \gamma (i_{\text{total}}[k])^2 + p T_{\text{amb}}[k]$$

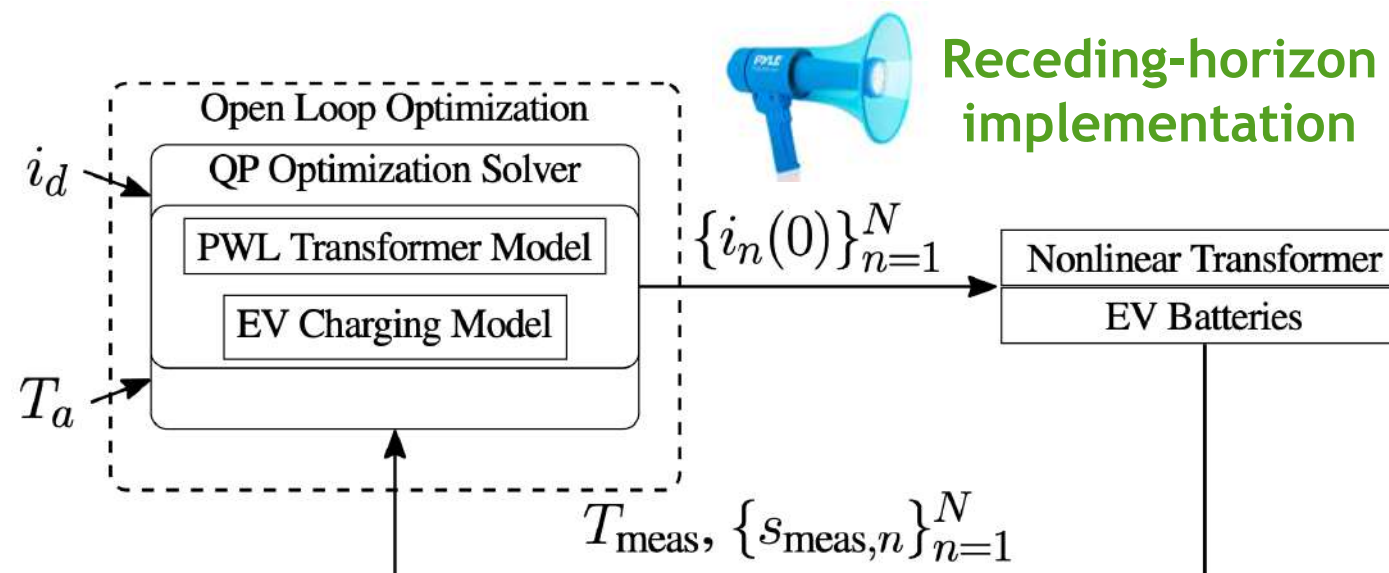
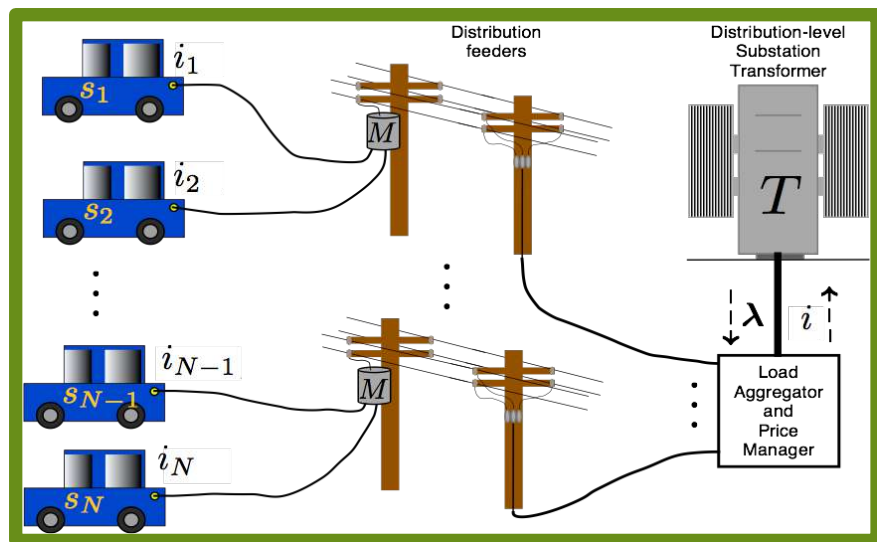
**Aggregate current:**

$$i_{\text{total}}[k] = i_{\text{bgd}}[k] + \sum_{n=1}^N i_n[k]$$



# EV charging scenario: direct load control

With full information (EV + Transformer), solve open-loop optimal control problem



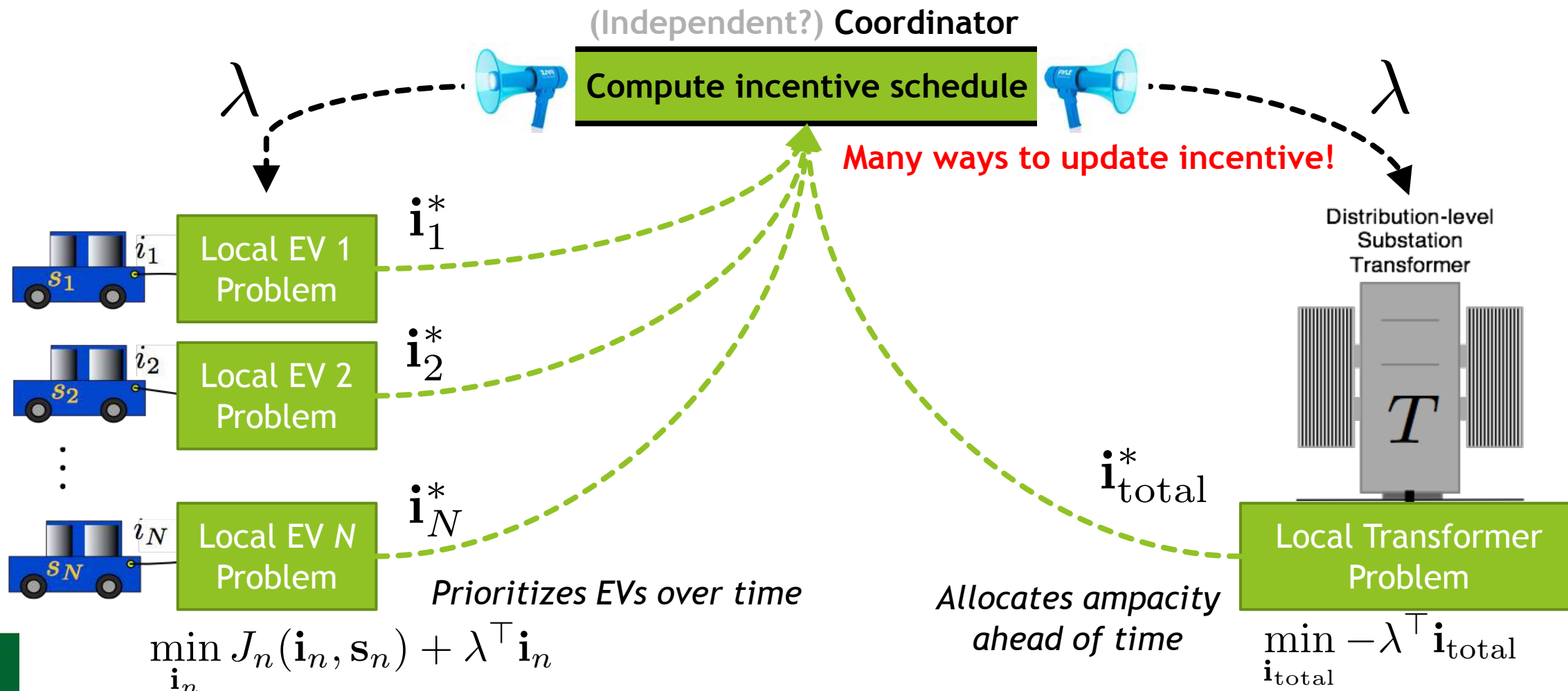
$$\min_{i_n[k]} \sum_{n=1}^N \sum_{k=0}^{K-1} q_n(s_n[k+1] - 1)^2 + r_n(i_n[k])^2 =: \sum_{n=1}^N J_n(\mathbf{i}_n, \mathbf{s}_n)$$

*charge quickly!*      *limit high currents*

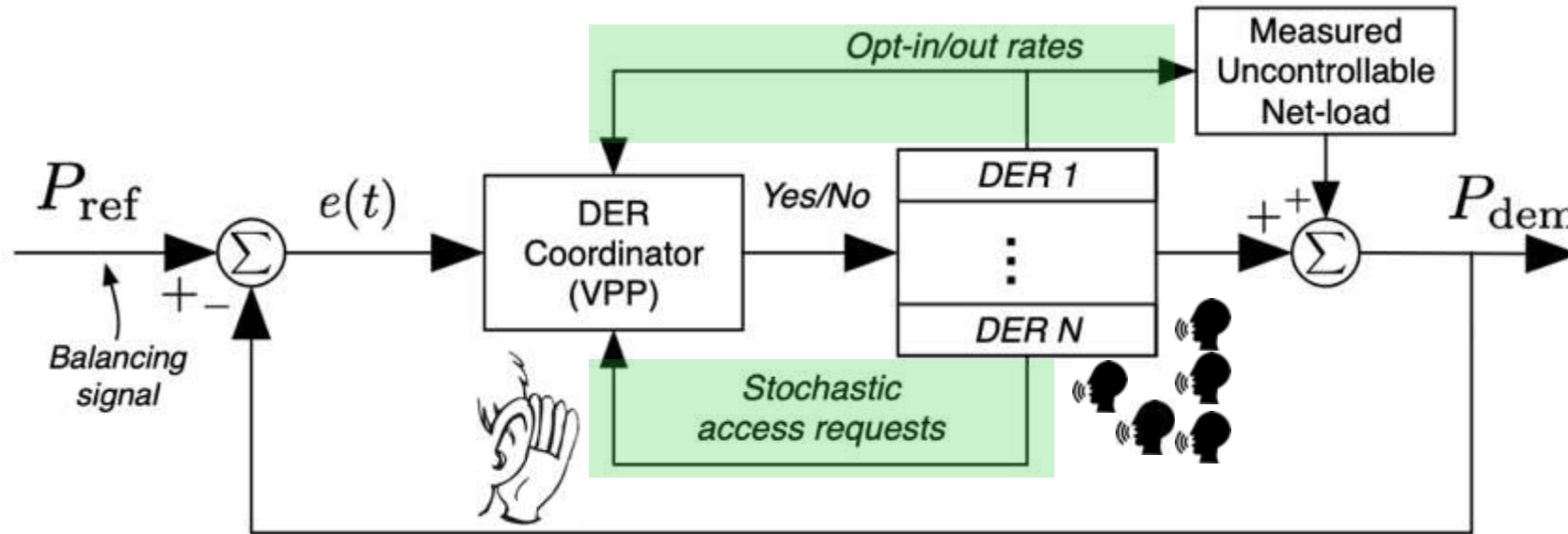


# EV charging scenario: indirect load control

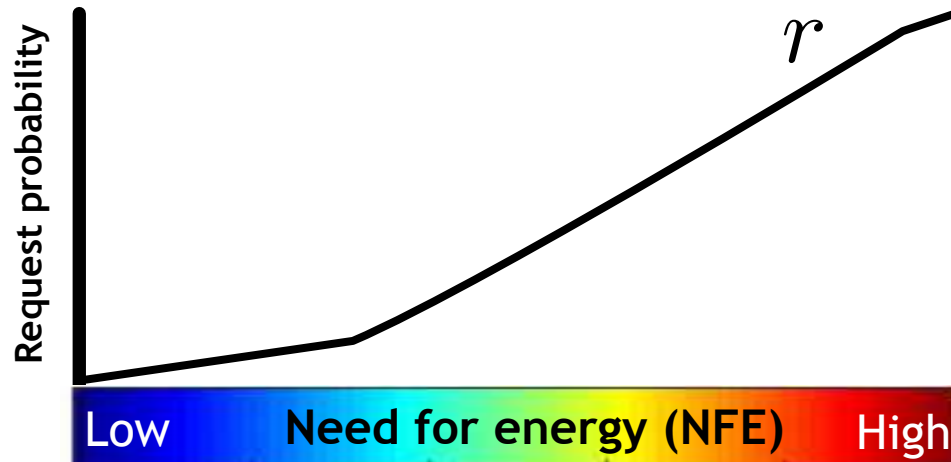
With limited information (EVs' do not share specs), solve distributed control problem



# Architecture #2: Device-driven approach (bottom-up)



Local device  
logic can  
guarantee QoS



Leverage **asynchronous** device-to-cloud comms to have devices **request** temporary access to grid

Controller processes **all** incoming requests, so can **estimate total demand of fleet (feedback)**

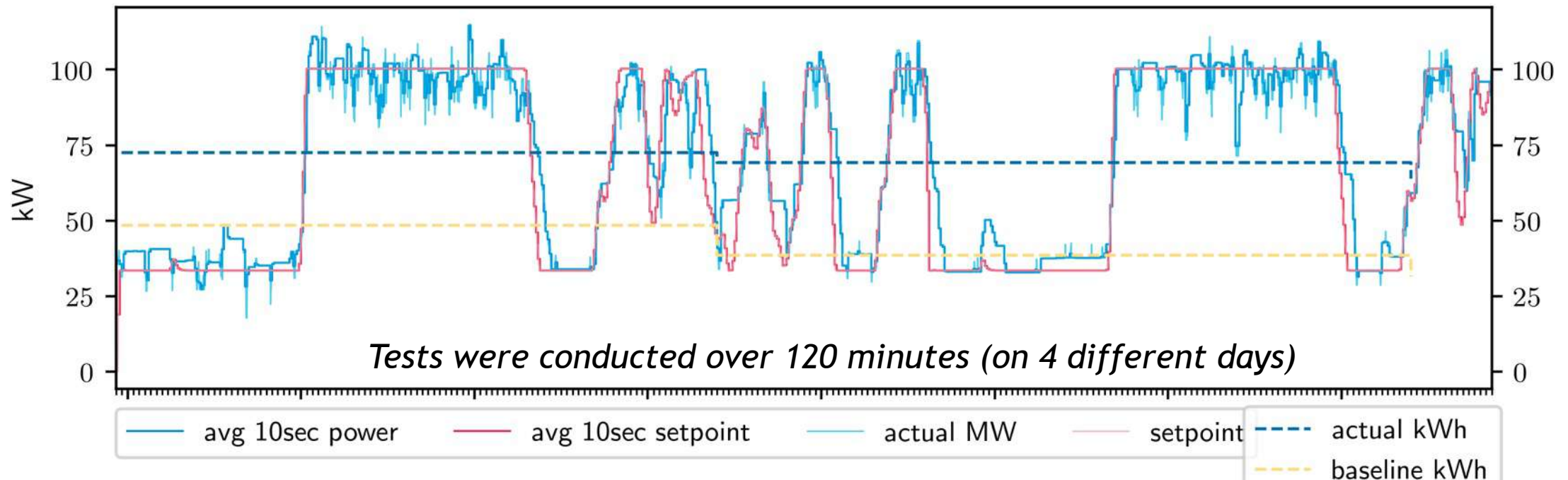
Request logic can include device constraints to manage **device health, QoS**, and can embed local network location to enable **network-aware coordination**



# Example: field trial with 200+ loads in 2021

## PEM demonstrates frequency regulation!

ARPA-E FastTracker Demo Power Data



### Pay-for-performance:

PJM Performance score

accuracy	delay	precision	composite
0.9509	0.9948	0.8281	0.9246

*Better than PJM's avg system performance (80-90%) and outperforms all assets but MW-scale energy storage*



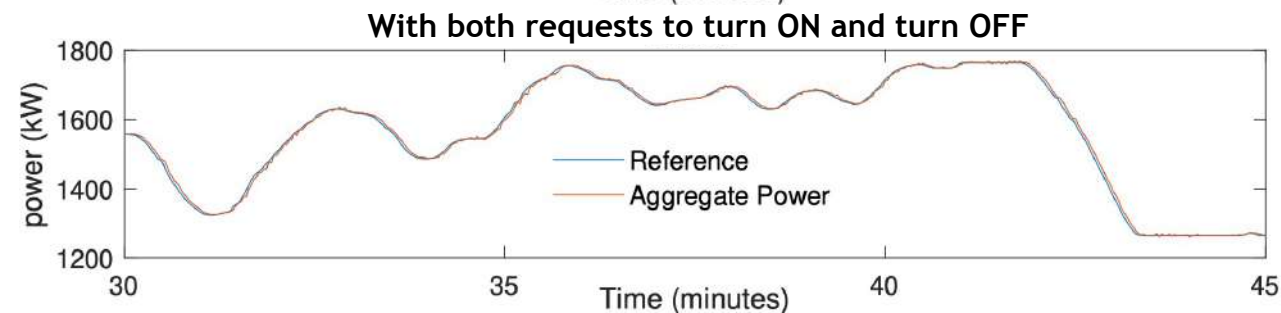
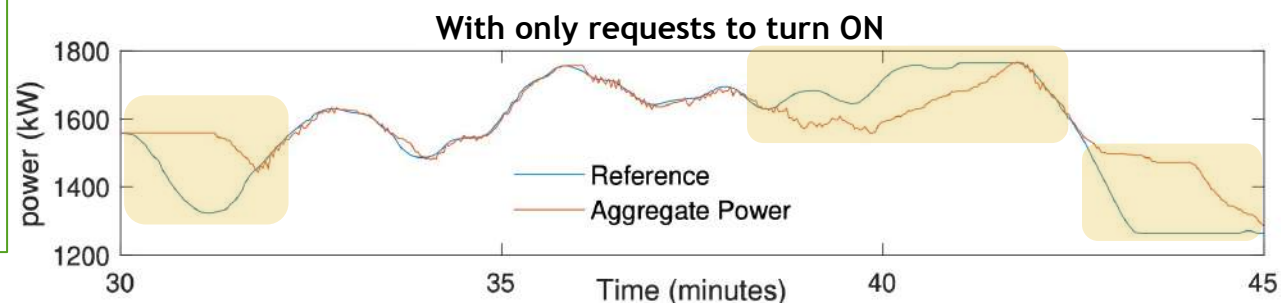
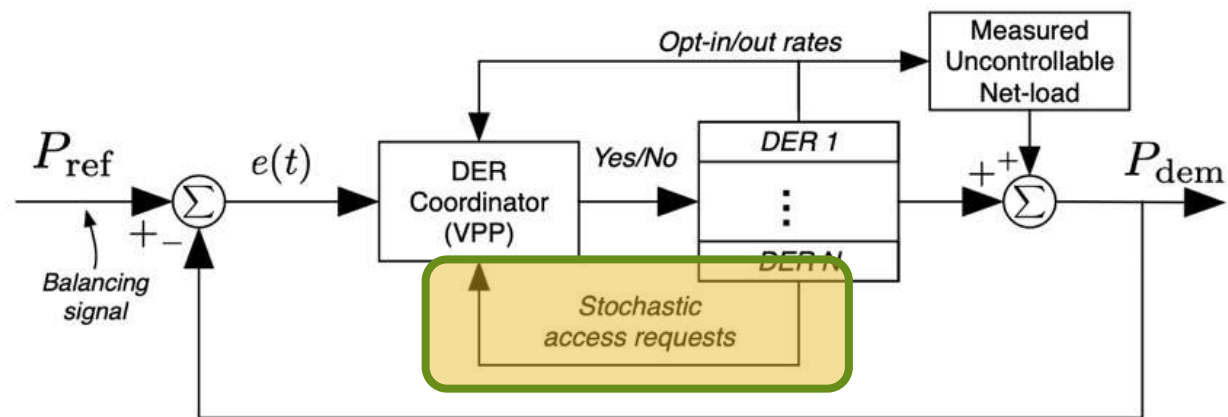
# New device-level logic enhances fleet's performance

## Control of Aggregate Air-Conditioning Load using Packetized Energy Concepts

Oluwagbemileke Oyefeso, Gregory S. Ledva, Mads Almassalkhi, Ian A. Hiskens, and Johanna L. Mathieu

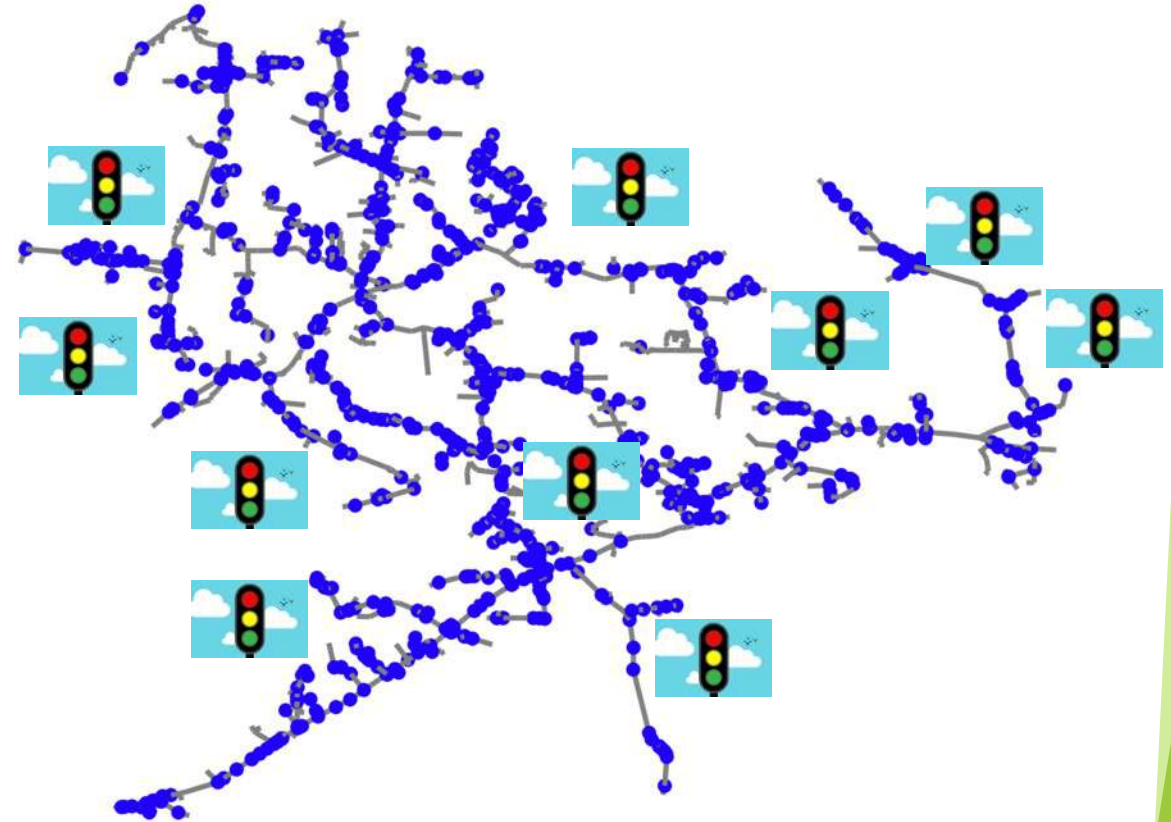
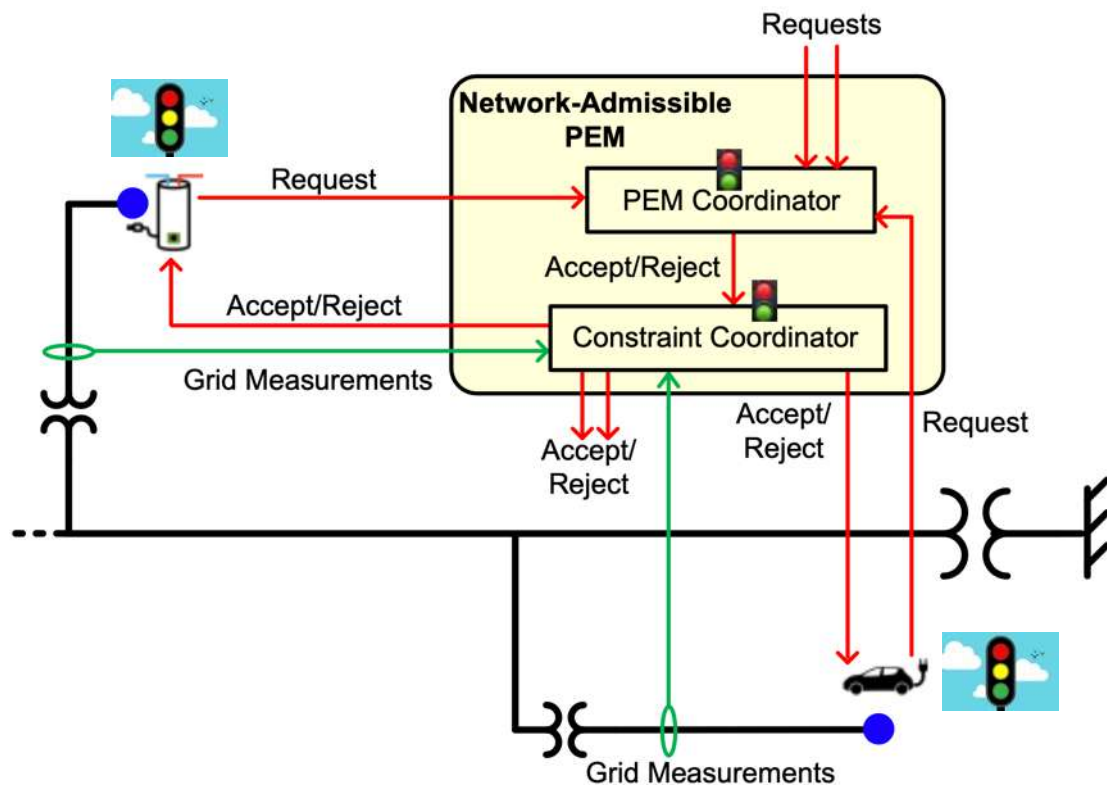
**Abstract**—The paper extends the packetized energy management (PEM) control strategy to enable coordination of compressor-based thermostatically controlled loads (TCLs), such as air conditioners. This establishes a new method of harnessing the flexibility of this ubiquitous resource, enabling a variety of grid services, such as frequency regulation. In the original PEM scheme, resources request energy packets and turn on if their request is approved. That PEM scheme has been further extended by introducing the concept of turn-off requests. We find that this increases flexibility and improves tracking performance. Through a case study involving over 1000 air conditioners, we evaluate the performance of a population of TCLs providing frequency regulation under PEM, highlighting both the capabilities and limitations. Simulations indicate our controller extensions significantly increase resource availability and tracking performance. We show that it is possible to achieve RMS tracking error below 2% when providing more than 250 kW of frequency regulation.

$t_{\text{locked}}^{\text{on}}$	Compressor turn-on lock-out time [s].
$t_{\text{locked}}^{\text{off}}$	Compressor turn-off lock-out time [s].
$t_{\text{min}}^{\text{on}}$	Energy packet minimum epoch length [s].
$t_{\text{max}}^{\text{on}}$	Energy packet maximum epoch length [s].
$t_{\text{comp}}$	Compressor lock-out timer [s].
$t_n$	Elapsed epoch time for AC $n$ [s].
$T_a$	Indoor Air Temperature [°C].
$T_m$	Inner Mass Temperature [°C].
$T_o$	Outdoor Air Temperature [°C].
$T_n^{\text{set}}$	Temperature set-point [°C].
$T_n^{\text{min}}$	Lower dead-band temperature [°C].
$T_n^{\text{max}}$	Upper dead-band temperature [°C].
$U_a$	Conductance of building envelope [kW/°C].



# Augmenting device logic with local grid data

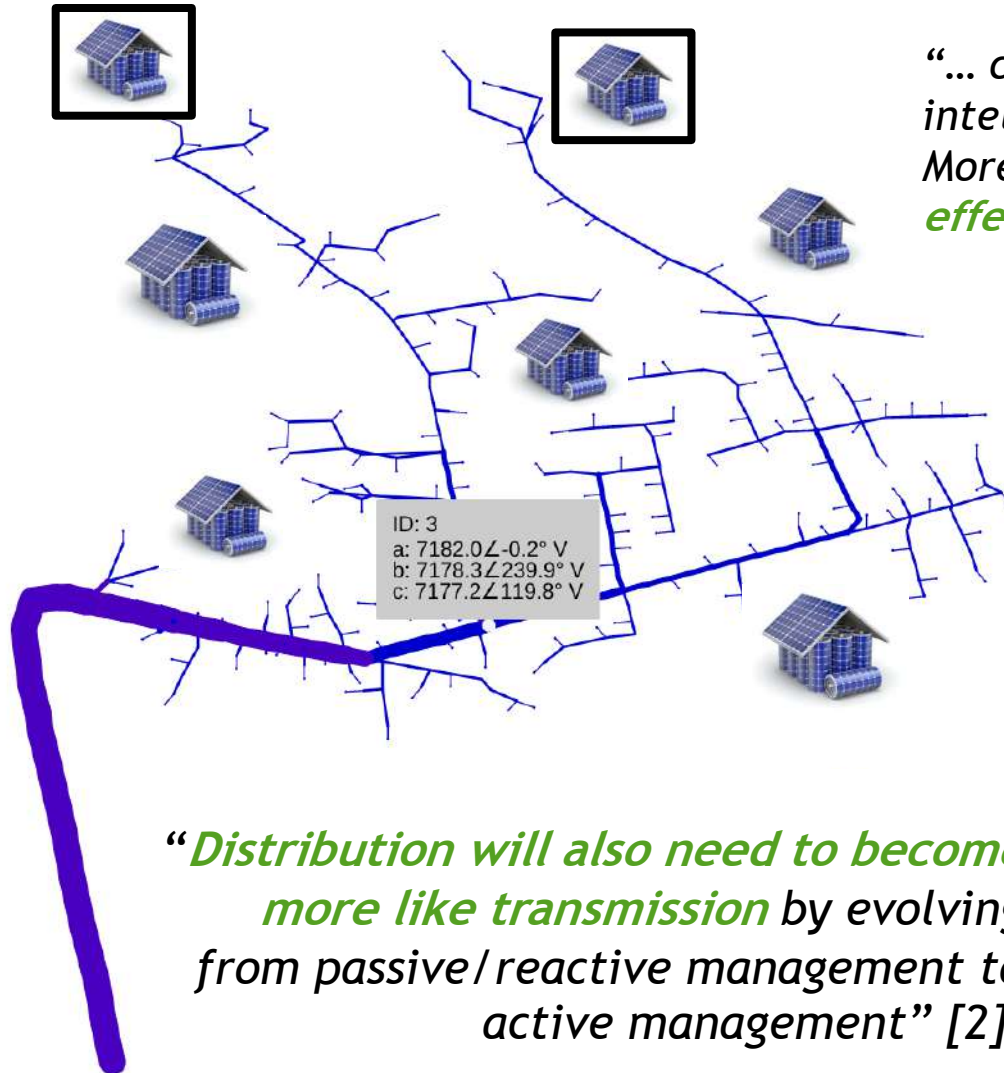
Local sensing augments device logic with live grid conditions + traffic-light device logic



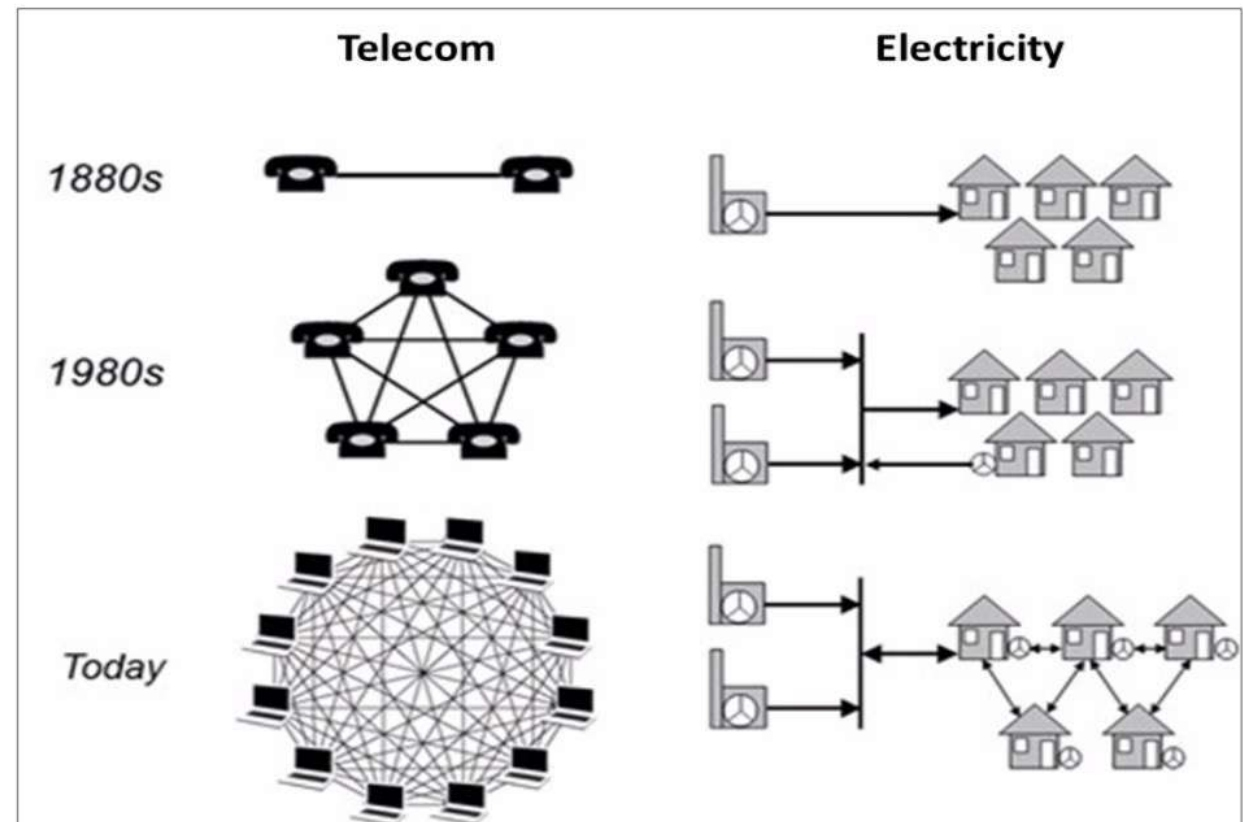
**Many open questions:** measurement types, locations, update rates, data integrity, etc...



# What active role should the grid operator play?



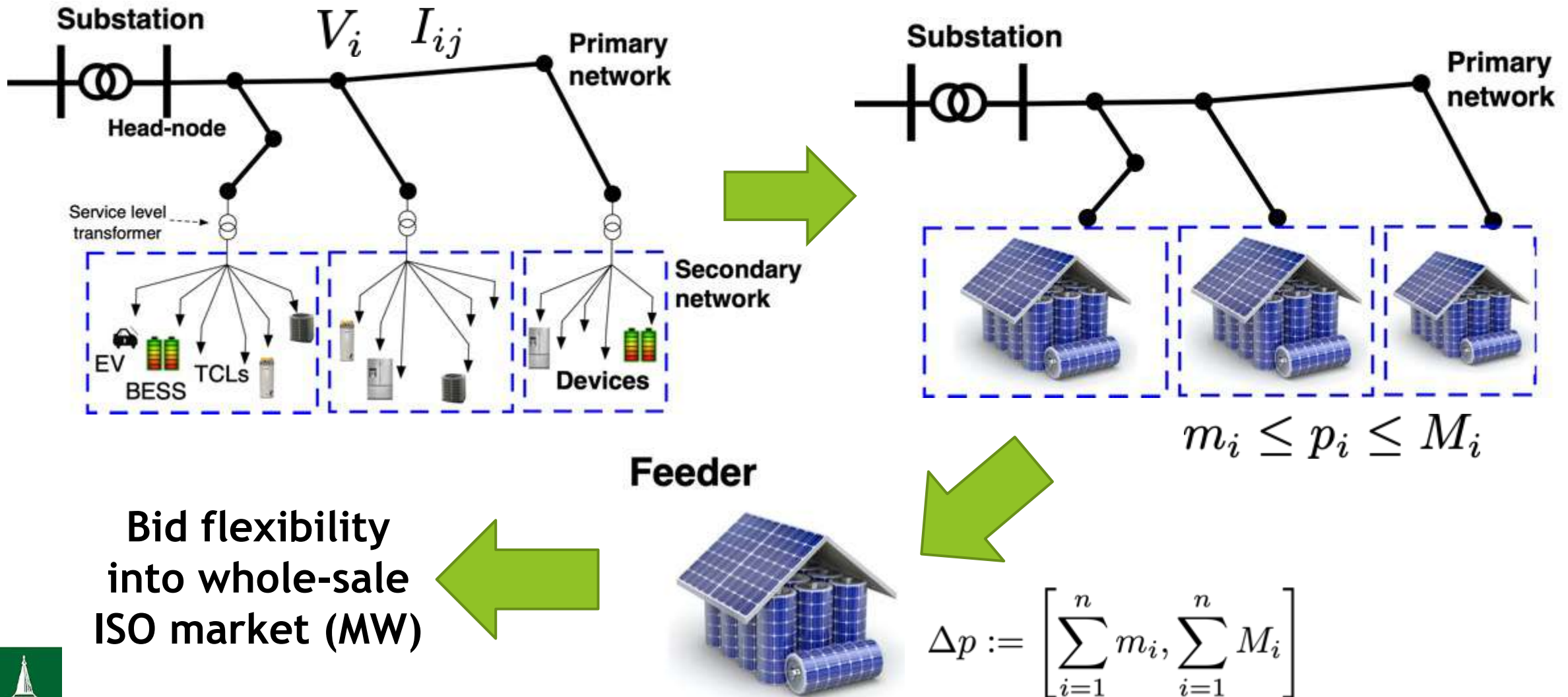
“... create open networks that increase value through the interaction of intelligent devices on the grid and prosumerization of customers  
Moreover, even *greater value can be realized through the synergistic effects of convergence of multiple networks*” [1].



“*Distribution will also need to become more like transmission* by evolving from passive/reactive management to active management” [2].



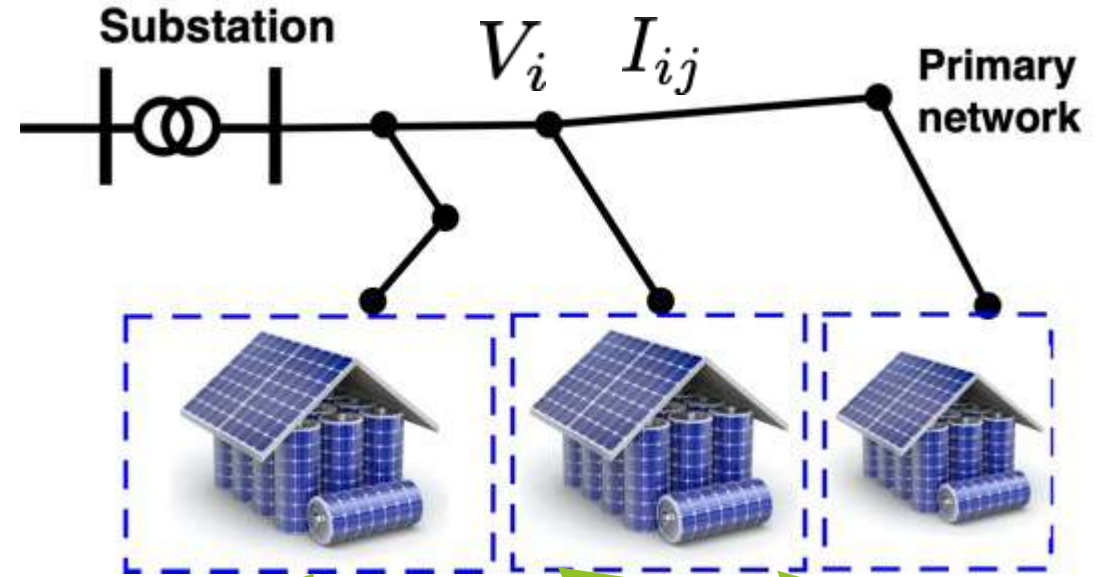
# Motivating example: aggregating flexible resources



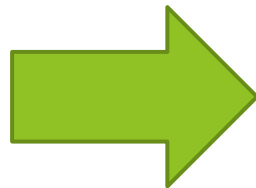
# Motivating example: disaggregating flexible resources

## Can we solve disaggregation in real-time?

- Solve grid optimization problem repeatedly
- + Guarantees grid reliability!
- Can DisAgg problem be solved fast [W, X, Y, Z]?
  - Can we provide admissibility guarantees?



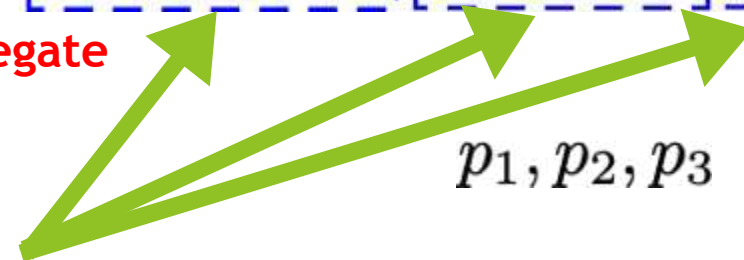
Requested  
flexibility from  
ISO (MW)



Feeder



Disaggregate

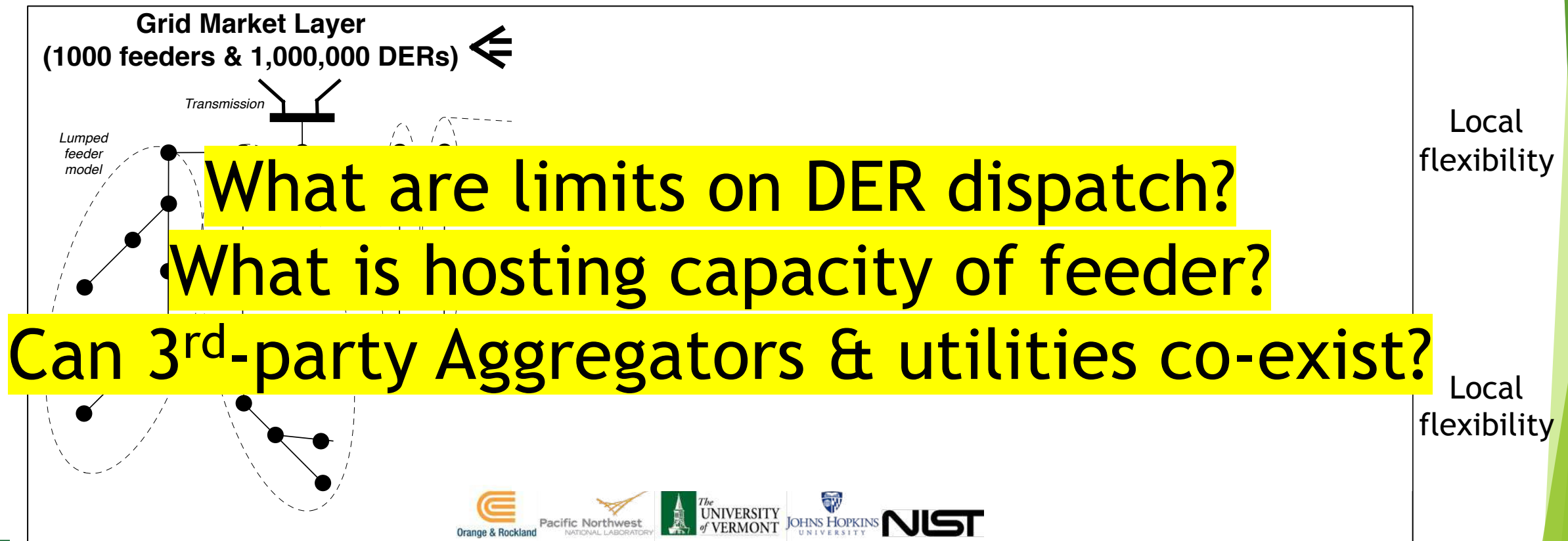


$p_1, p_2, p_3$



# Past experiences with "utility-centric" approaches

**Utility-centric = utility does it all:** network ops, DER coordination/dispatch, markets



[W] Almassalkhi, et al, "Hierarchical, Grid-Aware, and Economically Optimal Coordination of Distributed Energy Resources in Realistic Distribution Systems," Energies, 2020.

[X] Nawaf Nazir, Pavan Racherla, and Mads Almassalkhi, "Optimal multi-period dispatch of distributed energy resources in unbalanced distribution feeders", IEEE Trans. on Power Systems, 2020

[Y] Nawaf Nazir and M. Almassalkhi, "Voltage positioning using co-optimization of controllable grid assets," IEEE Trans. on Power Systems, 2020.

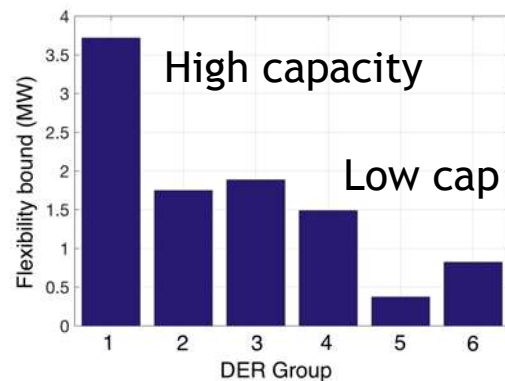
[Z] S. Brahma, Nawaf Nazir, et al, "Optimal and resilient coordination of virtual batteries in distribution feeders," IEEE Trans. on Power Systems, 2020



# Fundamental asymmetries in information & control

## Utility (grid information+data)

- Need to ensure grid reliability
- Need to protect grid data
- **Lack access to devices**
- **Knows grid capacity**



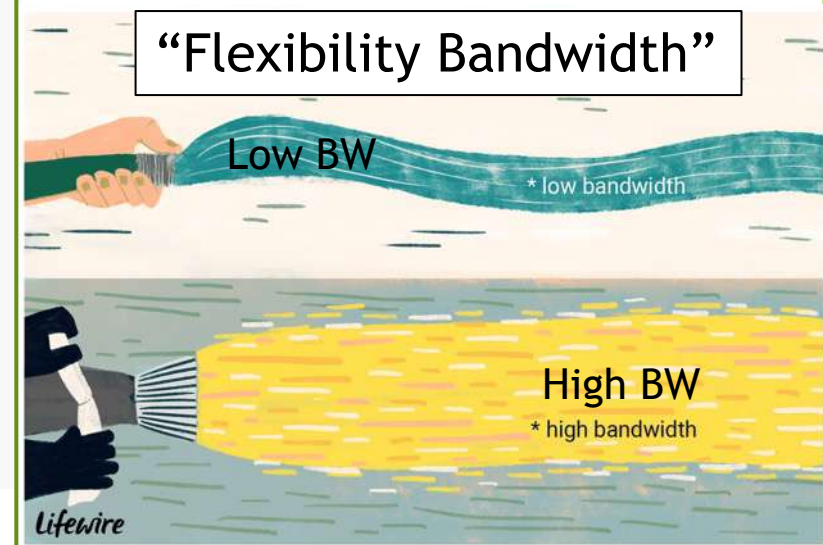
Prices to devices? DLMPs?



## Aggregators (device access, markets)

- Need to ensure device QoS
- Need to provide market services
- **Lacks access to grid data**
- **Knows device flexibility**

## “Flexibility Bandwidth”



Let's try something different!

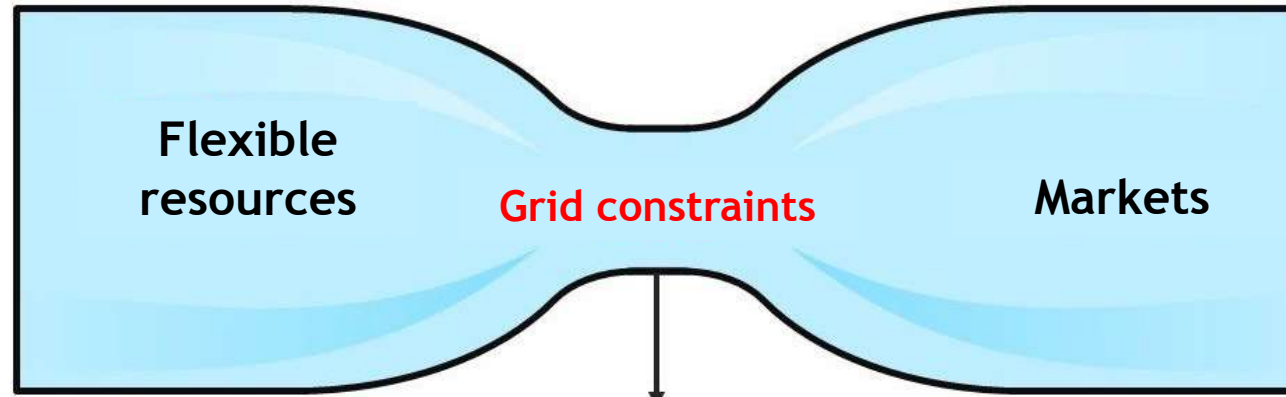




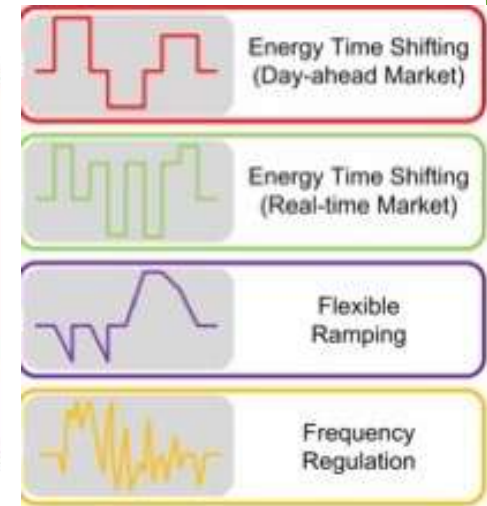
# Idea: *think like an internet service provider (ISP)*



**Aggregators:**  
flexibility from  
coordinated devices

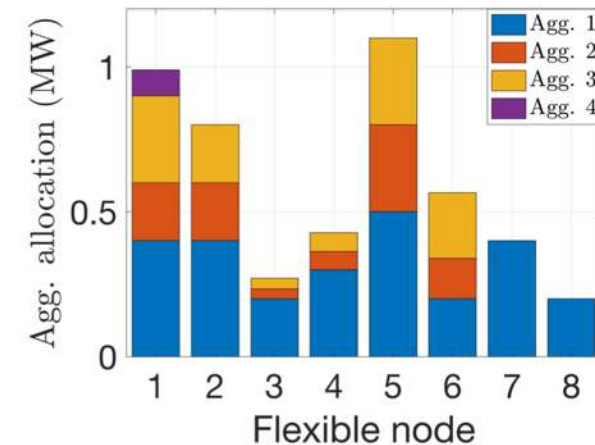
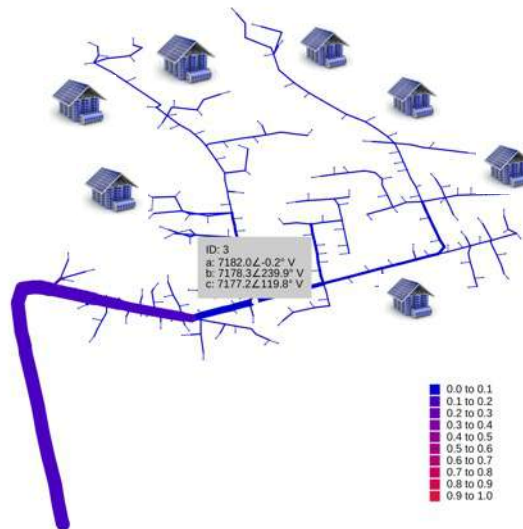


**Utility:** Decompose feeder HC at each node



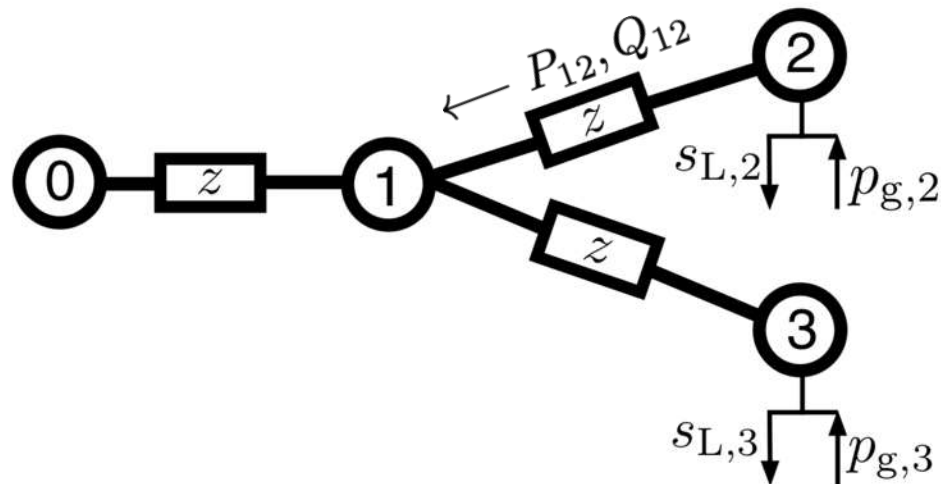
Aggregator is allocated portion of available HC at node  $i$

Aggregator bids for priority access to HC



# Finding set of admissible (active) injections

- Simple 3-node balanced distribution feeder example with 2 controllable  $p_g$  nodes modeled by *DistFlow*:



$$v_i := |V_i|^2 \text{ and } l_{ij} := |I_{ij}|^2$$

$$v_j = v_i + 2r_{ij}P_{ij} + 2x_{ij}Q_{ij} - |z_{ij}|^2 l_{ij}$$

$$P_{ij} = p_j + \sum_{h:h \rightarrow j} (P_{jh} - r_{jh}l_{jh})$$

$$Q_{ij} = q_j + \sum_{h:h \rightarrow j} (Q_{jh} - x_{jh}l_{jh})$$

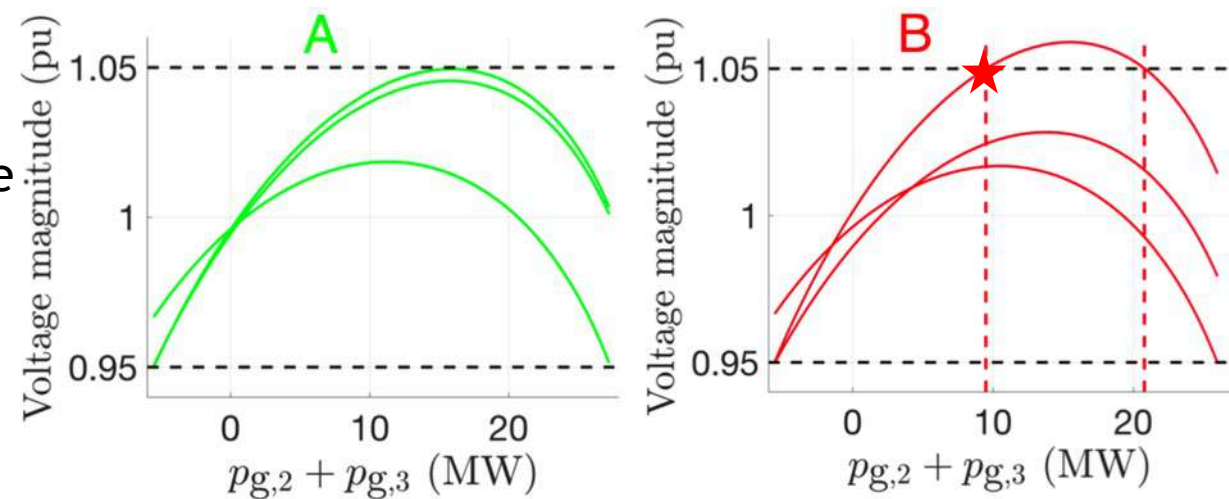
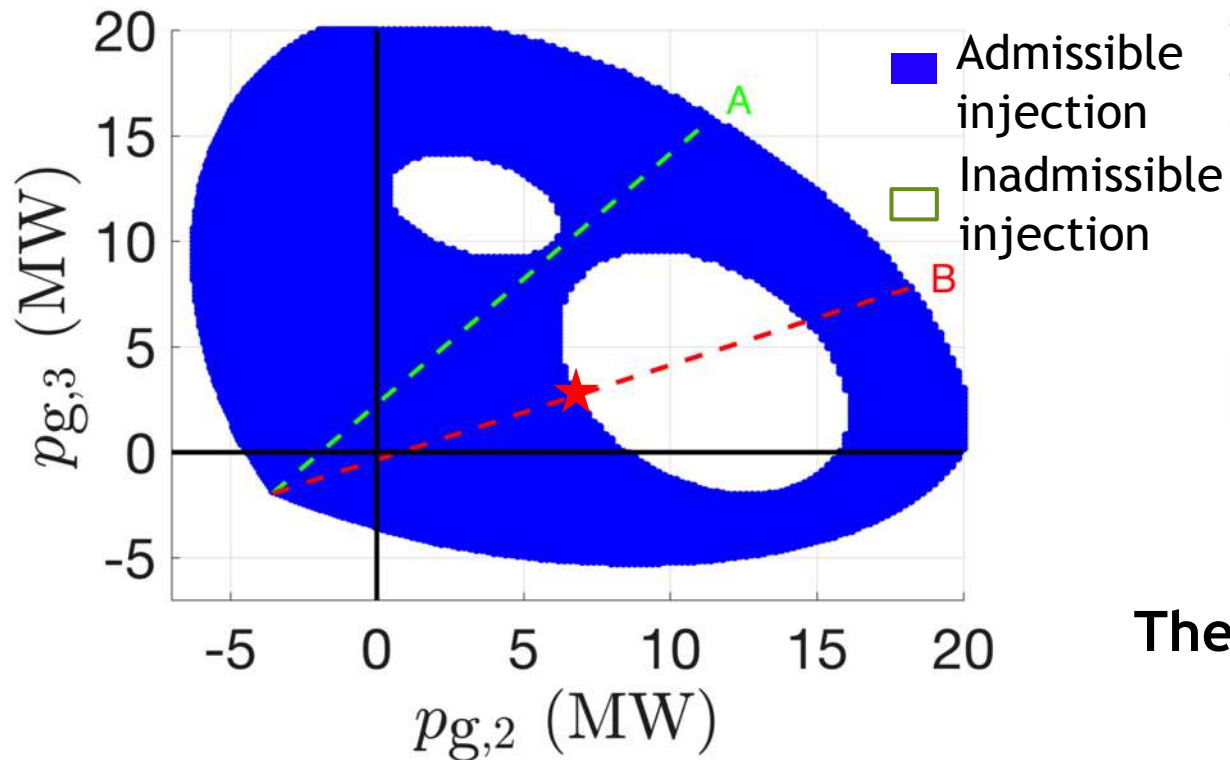
$$l_{ij}(P_{ij}, Q_{ij}, v_j) = \frac{P_{ij}^2 + Q_{ij}^2}{v_j}, \quad \text{The only nonlinear relation}$$

$$\text{Network limits: } v_i \in [\underline{v}_i, \bar{v}_i], l_{ij} \in [\underline{l}_{ij}, \bar{l}_{ij}]$$



# Finding set of admissible (active) injections

- Simple 3-node balanced distribution feeder example:



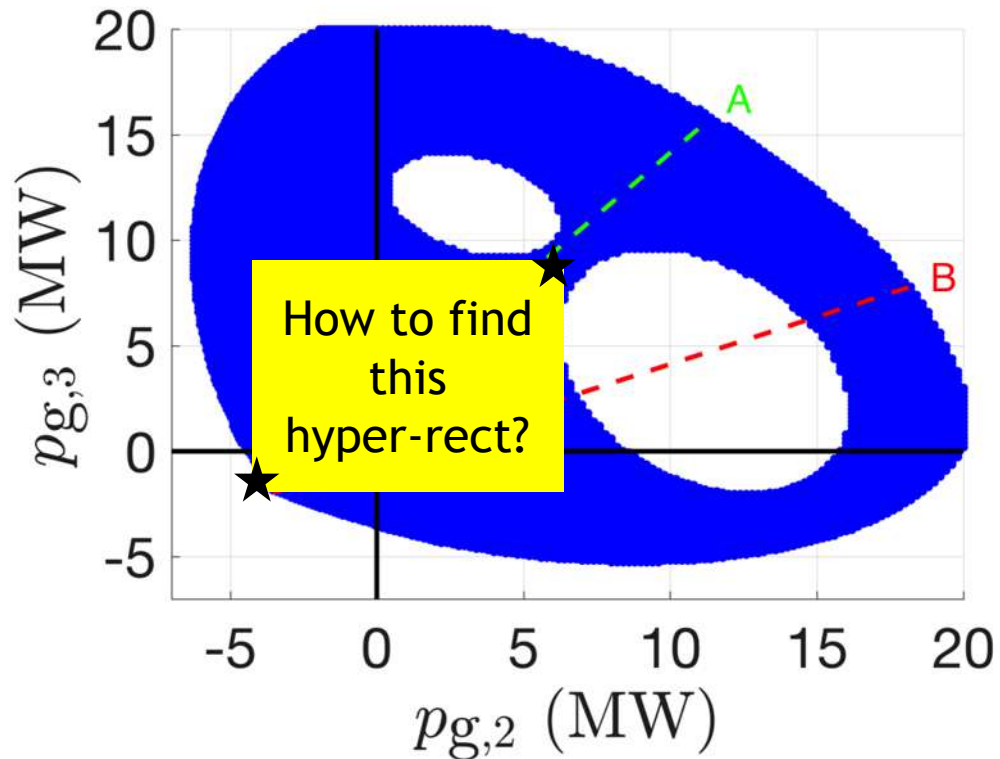
The two controllable active power resources are limited in aggregate by the network - i.e., their individual limits are coupled



Network limits:  $v_i \in [\underline{v}_i, \bar{v}_i], l_{ij} \in [\underline{l}_{ij}, \bar{l}_{ij}]$

# Finding set of admissible (active) injections

- Goal: find largest hyper-rectangle to determine  $p_g$  limits (decoupled)



■ Admissible injection  
■ Inadmissible injection

$$v_j = v_i + 2r_{ij}P_{ij} + 2x_{ij}Q_{ij} - |z_{ij}|^2 l_{ij}$$

$$P_{ij} = p_j + \sum_{h:h \rightarrow j} (P_{jh} - r_{jh}l_{jh})$$

$$Q_{ij} = q_j + \sum_{h:h \rightarrow j} (Q_{jh} - x_{jh}l_{jh})$$

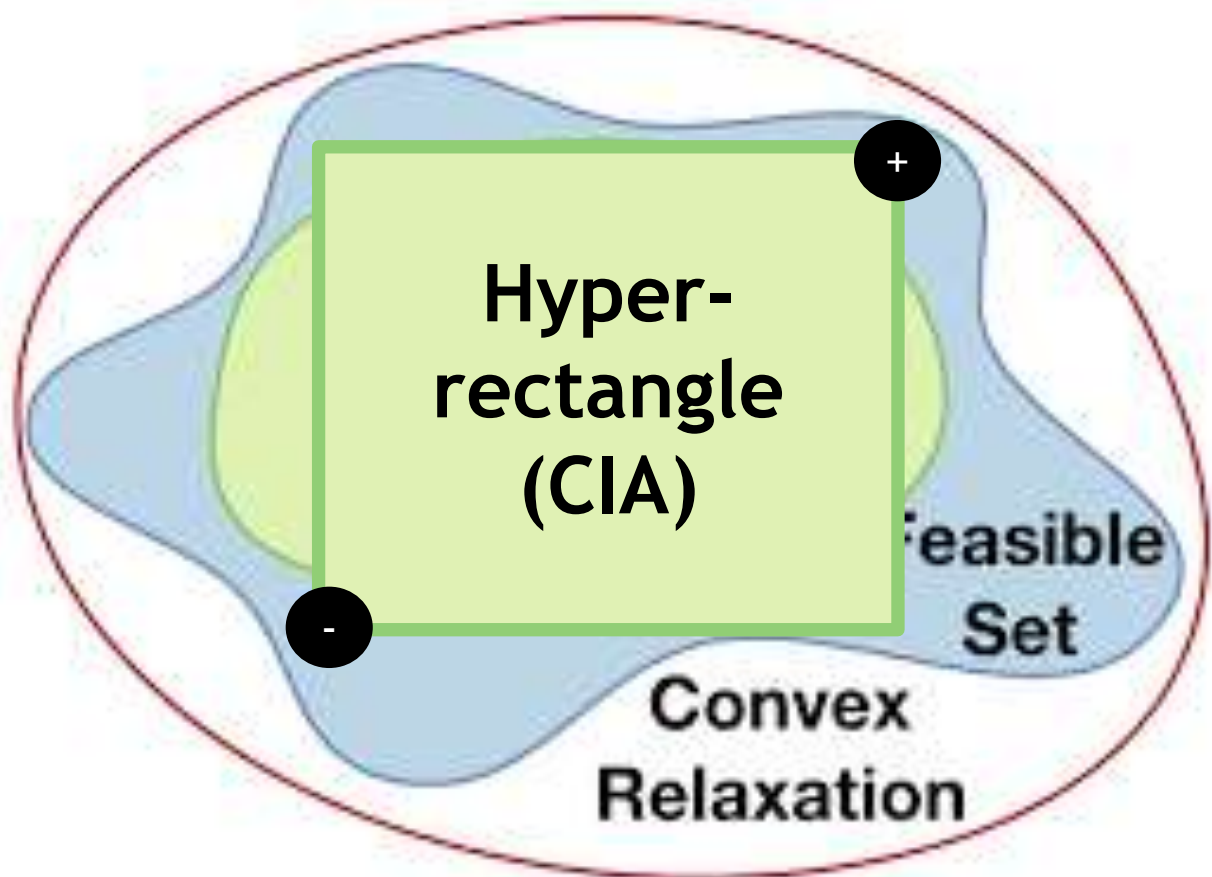
$$l_{ij}(P_{ij}, Q_{ij}, v_j) = \frac{P_{ij}^2 + Q_{ij}^2}{v_j},$$

**Idea:** replace non-convex constraint with a convex inner approximation (CIA)





# Convexity, optimality, and admissibility



**Feasible set** contains all dispatch solutions that are admissible (i.e., satisfy all NLP constraints)

**Convex relaxation** contains feasible set + some solutions may not be not admissible at optimality.

**Convex inner approximation (CIA)** contains a convex subset of the admissible solutions (but is suboptimal).

Goal: find largest hypercube to determine HC

Approach: eliminate **non-convexity** via convex bounds

$$\underbrace{l_{lb,ij}} \leq \underbrace{l_{ij}(P_{ij}, Q_{ij}, v_j) = \frac{P_{ij}^2 + Q_{ij}^2}{v_j}}_{\text{convex}} \leq \underbrace{l_{ub,ij}}$$

Shown to be affine

Shown to be convex

Original Image source: D. Lee, H. D. Nguyen, K. Dvijotham and K. Turitsyn, "Convex Restriction of Power Flow Feasibility Sets," in *IEEE Transactions on Control of Network Systems*, vol. 6, no. 3, pp. 1235-1245, Sept. 2019.



For mathematical details, please see:

Nawaf Nazir and Mads Almassalkhi. "Grid-aware aggregation and real-time disaggregation of distributed energy resources in radial networks," *IEEE TPWRS*, 2021.

# Convex inner approximation and *proxy* variables

If we can find envelope  $l_{lb,ij} \leq l_{ij}(P_{ij}, Q_{ij}, v_j) = \frac{P_{ij}^2 + Q_{ij}^2}{v_j} \leq l_{ub,ij}$

Then, we can create *proxy* variables that upper (+) and lower (-) bound the physical (P, Q, V)

Given a nominal operating point,  $x_{ij}^0 := (P_{ij}^0, Q_{ij}^0, v_j^0)$

$$P^+ := Cp - D_R l_{lb}$$

$$P^- := Cp - D_R l_{ub}$$

$$Q^+ := Cq - D_{X+} l_{lb} - D_{X-} l_{ub}$$

$$Q^- := Cq - D_{X+} l_{ub} - D_{X-} l_{lb}$$

$$V^+ := v_0 \mathbf{1}_n + M_p p + M_q q - H_+ l_{lb} - H_- l_{ub}$$

$$V^- := v_0 \mathbf{1}_n + M_p p + M_q q - H_+ l_{ub} - H_- l_{lb}$$

$$l_{ij} \approx l_{ij}^0 + \mathbf{J}_{ij}^\top \delta_{ij} + \frac{1}{2} \delta_{ij}^\top \mathbf{H}_{e,ij} \delta_{ij}$$

$$\delta_{ij} := \begin{bmatrix} P_{ij} - P_{ij}^0 \\ Q_{ij} - Q_{ij}^0 \\ v_j - v_j^0 \end{bmatrix}, \quad \mathbf{J}_{ij} := \left[ \begin{array}{c} \frac{\partial l_{ij}}{\partial P_{ij}} \\ \frac{\partial l_{ij}}{\partial Q_{ij}} \\ \frac{\partial l_{ij}}{\partial v_j} \end{array} \right] \bigg|_{x_{ij}^0} = \begin{bmatrix} \frac{2P_{ij}^0}{v_j^0} \\ \frac{2Q_{ij}^0}{v_j^0} \\ -\frac{(P_{ij}^0)^2 + (Q_{ij}^0)^2}{(v_j^0)^2} \end{bmatrix}$$

$$\mathbf{H}_{e,ij} := \begin{bmatrix} \frac{2}{v_j^0} & 0 & \frac{-2P_{ij}^0}{(v_j^0)^2} \\ 0 & \frac{2}{v_j^0} & \frac{-2Q_{ij}^0}{(v_j^0)^2} \\ \frac{-2P_{ij}^0}{(v_j^0)^2} & \frac{-2Q_{ij}^0}{(v_j^0)^2} & 2\frac{(P_{ij}^0)^2 + (Q_{ij}^0)^2}{(v_j^0)^3} \end{bmatrix} \succeq 0^*$$

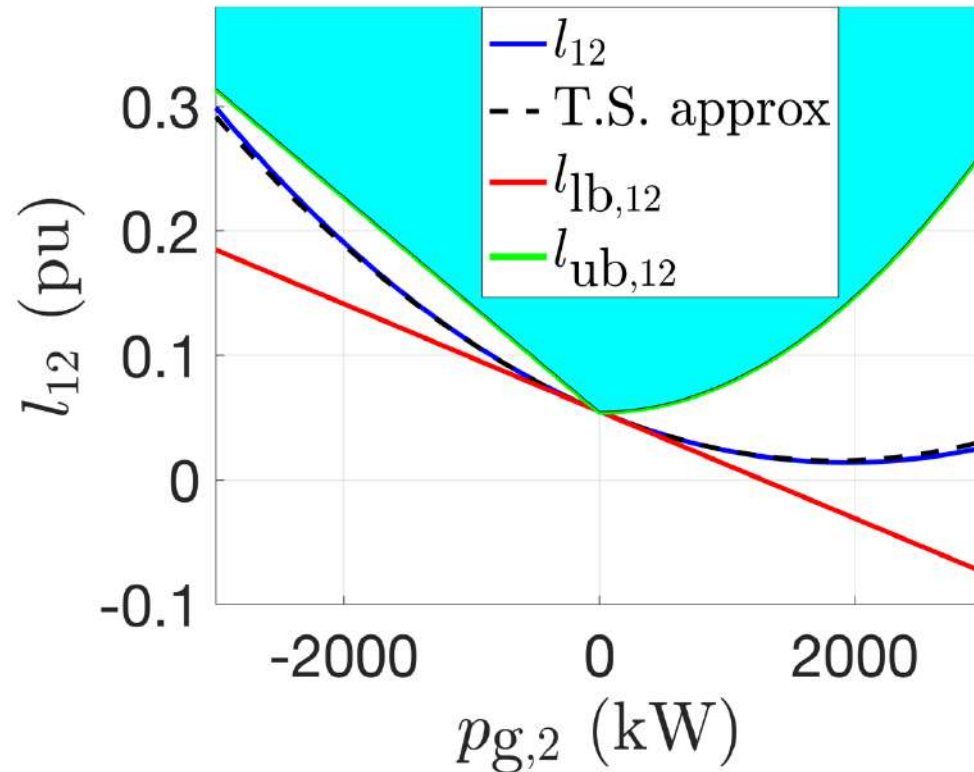
and from this model, we can explicitly define upper and lower bounds on  $l_{ij}$  that yield a convex inner approximation.



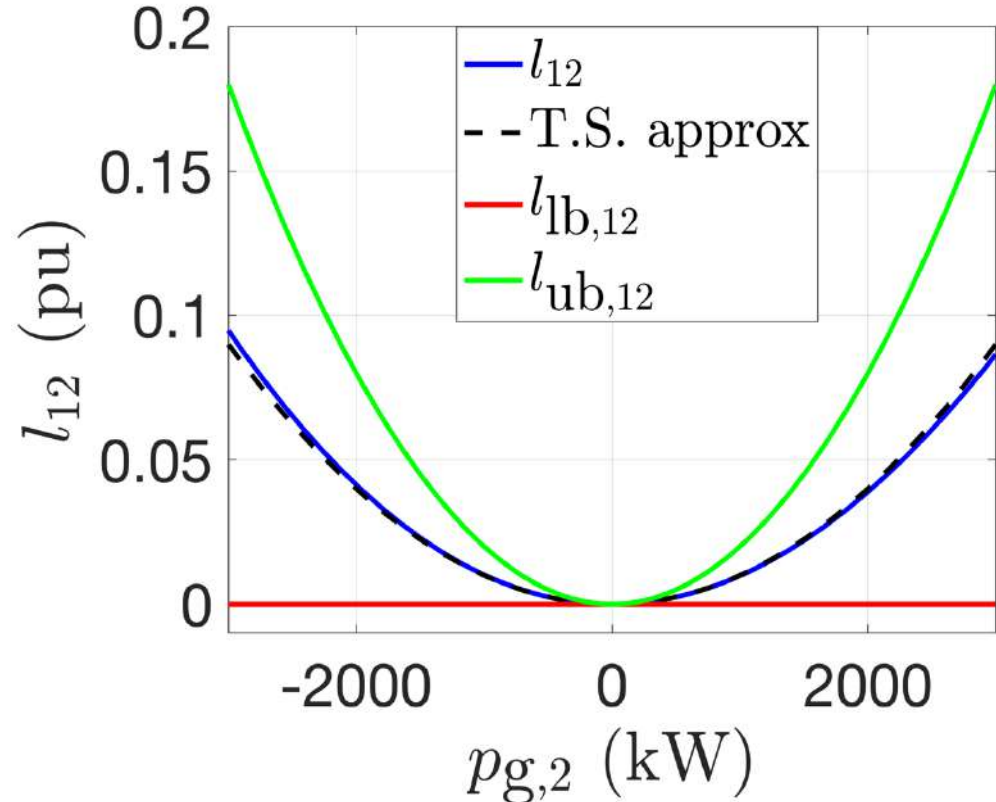
# Convex inner approximation via proxy variables

$$l_{lb,ij} \leq \boxed{l_{ij}(P_{ij}, Q_{ij}, v_j) = \frac{P_{ij}^2 + Q_{ij}^2}{v_j}}, \leq l_{ub,ij}$$

Full-load conditions



No-load conditions



For mathematical details, please see:

Nawaf Nazir and Mads Almassalkhi. "Grid-aware aggregation and realtime disaggregation of distributed energy resources in radial networks," IEEE TPWRS, 2021.

# Determining admissible injection limits

$p_i^+$  maximum active power injection at *each* node:

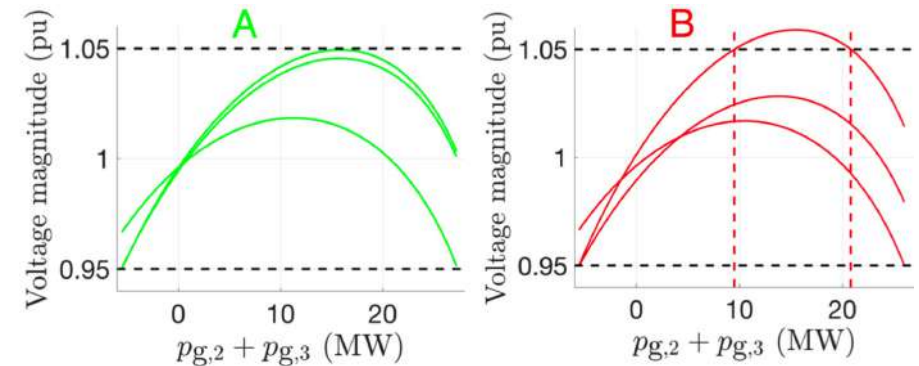
$$p^+(x^0) = \arg \max_p \sum_{i=1}^N f_i(p_i) \\ \text{s.t. } p \in \mathcal{X}(x^0)$$

$p_i^-$  minimum active power injection at *each* node:

$$p^-(x^0) = \arg \min_p \sum_{i=1}^N f_i(p_i) \\ \text{s.t. } p \in \mathcal{X}(x^0)$$

**Theorem:** If  $p_i \in [p_i^-, p_i^+] \forall i \Rightarrow \underline{V} \leq V^-(p) \leq V(p) \leq V^+(p) \leq \bar{V}$

Proof is conditioned upon:  $dV^+/dp, dV/dp \geq 0$



**Monotonicity conditions:**

More load  $\rightarrow$  higher voltage  
Less load  $\rightarrow$  lower voltage

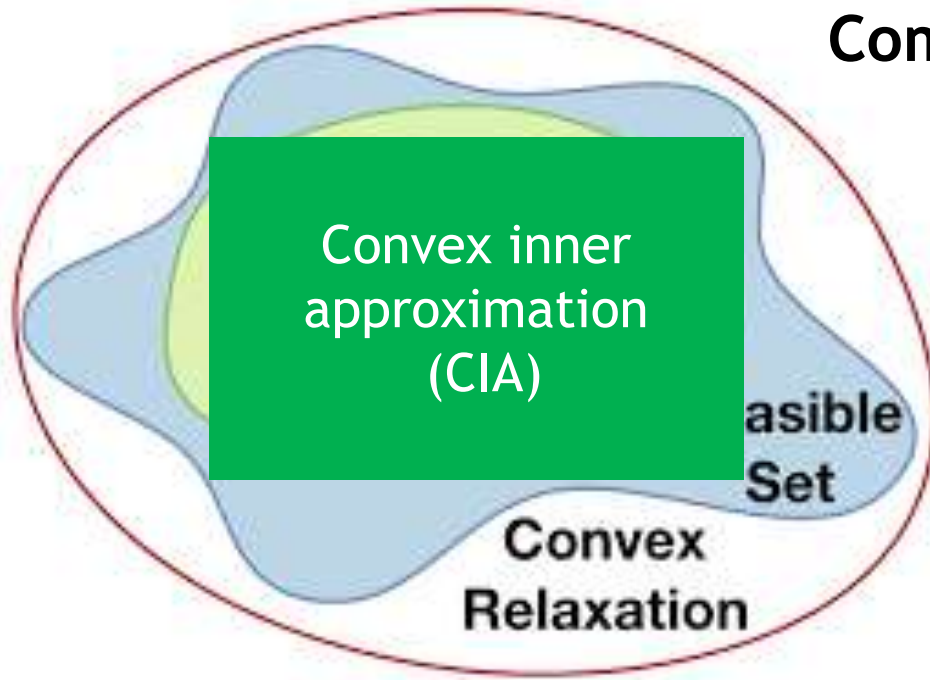
**Bonus:** objective is feeder's hosting capacity!





# What about conservativeness of CIA?

## Comparing grid flexibility bounds



System	CIA (MW)	NLP (MW)	CR (MW)
13-node	[-1.5, 9.1]	[-1.5, 9.7]	[-1.5, 12]
37-node	[-2.7, 5.3]	[-2.7, 5.3]	[-2.7, 16]
123-node	[-4.5, 13.9]	[-4.5, 14]	[-4.5, 24]

Convex relaxation (CR) over-estimates maximum reactive power capability

Nonlinear (NLP) has no optimality guarantees AND does not guarantee that entire range is admissible (i.e., no holes)

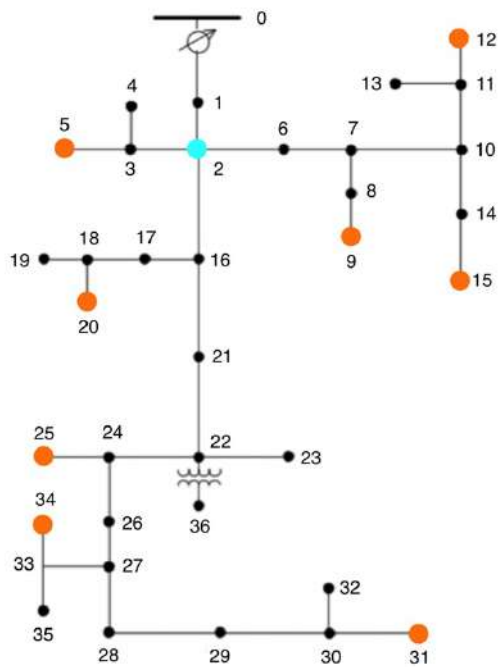
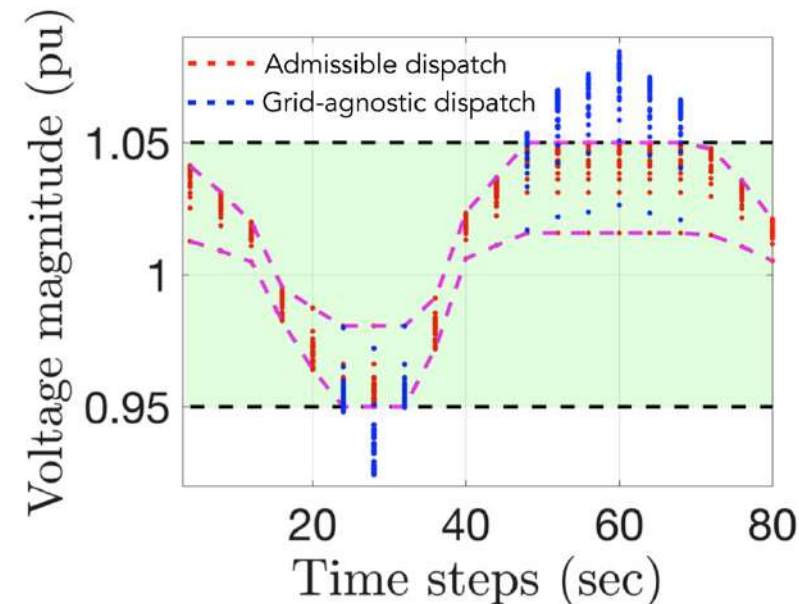
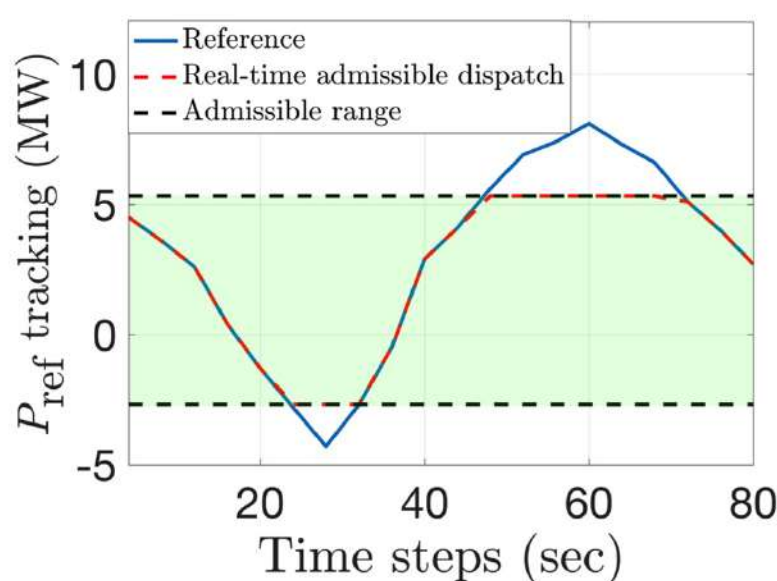
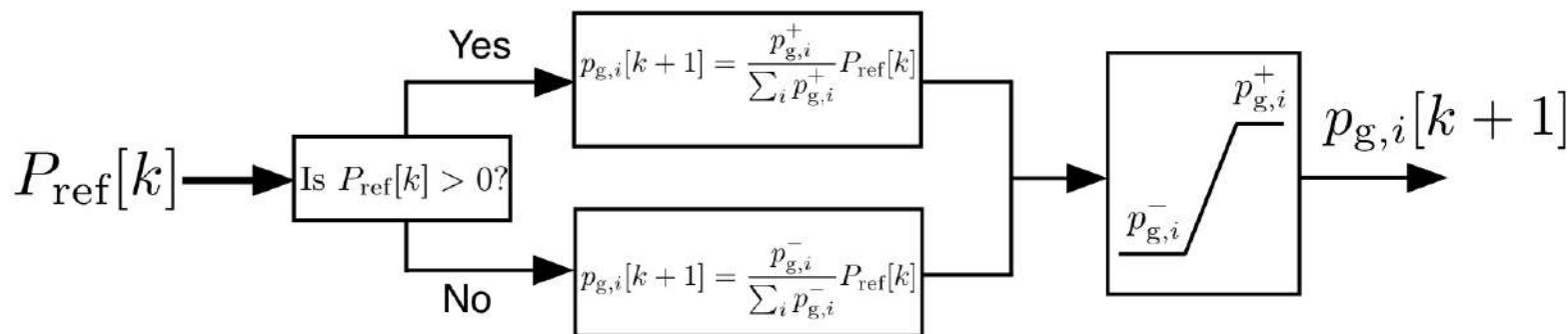
**Conclusion:** proposed (CIA) method is not overly conservative and entire range is admissible

Original Image source: D. Lee, H. D. Nguyen, K. Dvijotham and K. Turitsyn, "Convex Restriction of Power Flow Feasibility Sets," in *IEEE Transactions on Control of Network Systems*, vol. 6, no. 3, pp. 1235-1245, Sept. 2019.



# CIA enables real-time, grid-aware disaggregation

Nodal hosting capacities  $[p_i^-, p_i^+]$  enable an open-loop, distributed, and **grid-aware DER control policy**



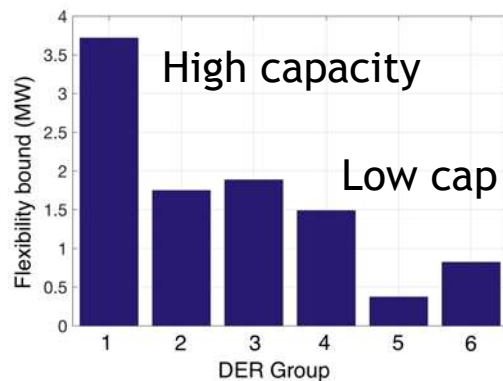
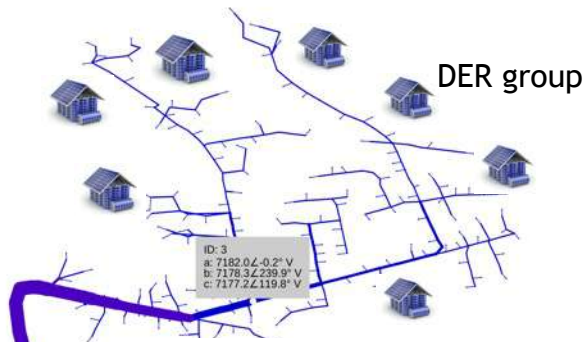
**IEEE 37-node network**  
(from Baker/Dall'Anese)



# Summary: DHC overcomes data/control asymmetry

## Utility (grid information+data)

- Dynamic hosting capacities capture grid conditions and limits



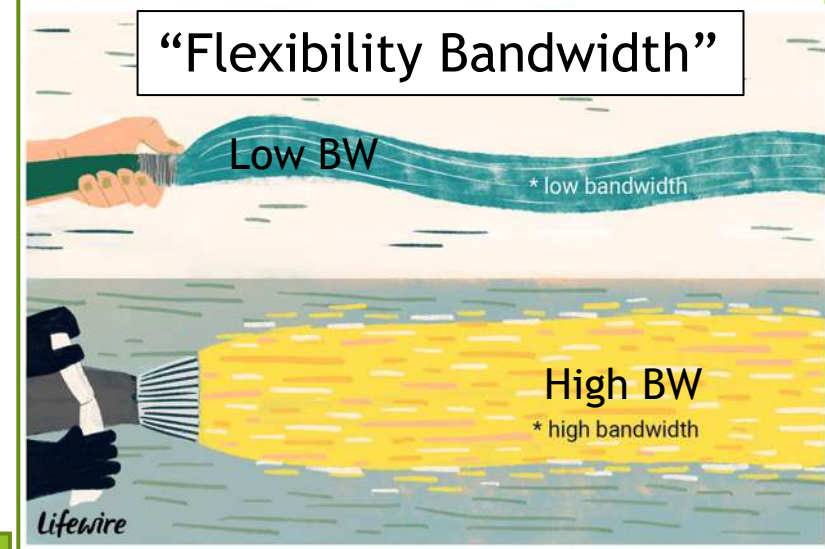
Available hosting capacity



Available flexibility

## Aggregators (device access, markets)

- Flexibility captures device availability and comfort limits







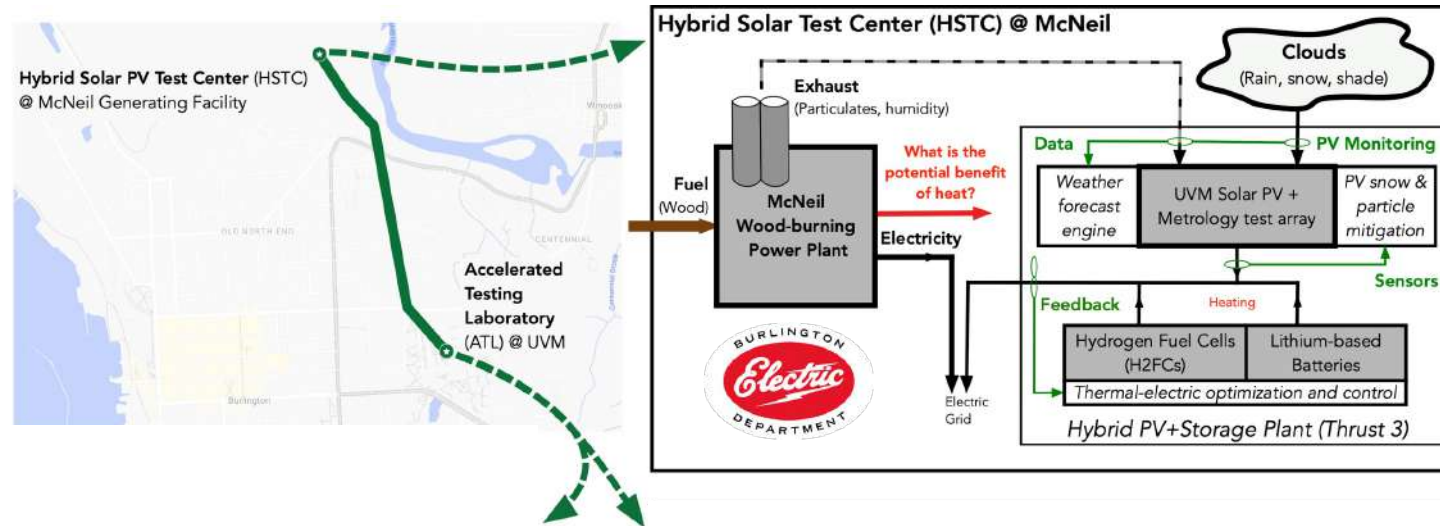
# Bonus topic: Hybrid Energy Systems

From virtual batteries to physical batteries

# What is a hybrid energy system?

Hybrid energy systems = *Coupling Heat + PV + Storage + Hydrogen + Power* = Lots of Data = Learning

HSTC = Hybrid  
Solar Test Center  
(1 mile from  
campus)



## Field deployment and validation of R&D

- thermal-electric modeling, control, optimization, operations, planning
- grid services
- reliability
- lifetime analysis





# Main objectives of DOE project (2023-2027)

## Long-term planning

1

Hybrid energy system **degradation and lifetime economics and performance**. Develop quasi-accelerated degradation models of solar PV in northern climates.

## Short-term operations

2

Optimize and control the hybrid energy system's performance across weather/climate conditions and **demonstrate advanced grid services** that support reliability and resilience across seasons.

## National impact

3

Develop nationally competitive energy research infrastructure in Vermont that supports national priorities around combating climate change & clean energy **workforce development**.





# DOE is looking for answers, too!

## Hybrid Energy Systems: Opportunities for Coordinated Research



### Markets, Policy, and Regulation Opportunities

The objectives of the markets, policy, and regulation research area are to evaluate regulations, policies, ownership structures, and market products that are emerging or needed to ensure efficient operation of HES. To relate the greater sense of urgency for the markets, policy, and regulation opportunities, they are presented prior to those for valuation and technology development; in contrast to conventional approaches in markets, policy, and regulation. This area provides a better understanding of the evolving development status, responding to the potential impacts of higher penetrations of HES on operations; improving the analysis of HES within interconnected systems; and providing analytical and technical support to state regulatory agencies.



#### Markets Database

Synthesize and disseminate current



#### HES Integration Studies

Analyze the impacts of



### Technology Development Opportunities



#### Controls Development and Testing

Expand efforts to develop robust and efficient control solutions for additional technology combinations and service types, and improve coordination for related research activities across DOE offices.



#### Plant-Level Design Optimization

Improve coordination across efforts to develop methods and tools for evaluating the optimal sizing, linkages, and operations of HES for a wide array of technology combinations.



#### Components Development and Testing

Coordinate efforts to develop and test power electronics, devices, communications, heat exchangers, and intermediate loops for application at various time steps, leveraging recent and ongoing capabilities development for independent technologies.



### Valuation Opportunities

The valuation research area focuses on tools, methods, and metrics for quantifying the value that different HES can provide, given hybrid system configuration, energy system, and market characteristics. HES come in a variety of types, are used in a variety of applications, and produce a variety of products. Comprehensive and harmonized valuation methodologies that encapsulate these variations are essential for determining which HES, if any, can best meet the needs of the electric and broader energy system. Opportunities are presented and organized in terms of identifying sources of value, developing consistent metrics and methodologies, and applying tools to estimate HES value over different scales and time horizons.



#### Sources of Value

Enhance information sharing across recent and ongoing HES research in different DOE offices to achieve harmonized value definitions and categories.



#### Methodologies and Metrics to Measure Value

Establish common methods and metrics for evaluating candidate HES to enable an apples-to-apples comparison of candidate HES.



#### Estimating Value

Estimate the value that HES can provide through analyses that expand and leverage past and ongoing research for select technology combinations.

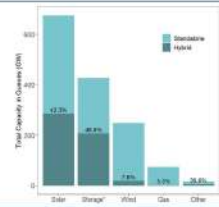
### High-Level Findings: 2021 Was a Big Year for Hybrids in the US

Hybrid / co-located plants exist in many configurations and are distributed broadly across the U.S.

- PV+Storage dominates in terms of number of plants (140), storage capacity (2.2 GW), and storage energy (7 GWh)
- There is now more battery capacity operating within PV+Battery hybrids than on a standalone basis
- Storage:generator ratios are higher and storage durations are longer for PV+Storage plants than for other types of generator+storage hybrids

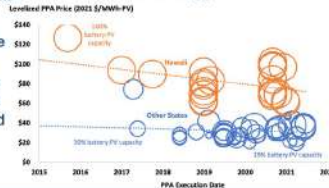
Hybrids comprise a large and growing share of proposed plants

- 42% (285 GW) of all solar and 8% (19 GW) of all wind in interconnection queues are proposed as hybrids (up from 34% and 6% in 2020)
- PV+storage dominates the hybrid development pipeline (at >90%)
- Proposed plants are concentrated in the West and CAISO



Prices from a sample of 67 PV+Storage PPAs in 10 states totaling 8.0 GW<sub>AC</sub> of PV and 4.5 GW<sub>AC</sub> / 18 GWh of batteries suggest that:

- Levelized PPA prices have declined over time
- But "levelized storage adders" for PV+Battery plants on the mainland have recently increased





# Thank you! Questions? Comments?



malmassa@uvm.edu



@theEnergyMads



<https://madsalma.github.io>

Traditional demand response



Today's flexibility: *not your parent's DR*

